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A Comparison of Singlet Oxygen Explicit Dosimetry (SOED) and Singlet Oxygen Luminescence Dosimetry (SOLD) for Photofrin-Mediated Photodynamic Therapy

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Abstract: Accurate photodynamic therapy (PDT) dosimetry is critical for the use of PDT in the treatment of malignant and nonmalignant localized diseases. A singlet oxygen explicit dosimetry (SOED) model has been developed for in vivo purposes. It involves the measurement of the key components in PDT—light fluence (rate), photosensitizer concentration, and ground-state oxygen concentration ([O2])—to calculate the amount of reacted singlet oxygen ([O2]rx), the main cytotoxic component in type II PDT. Experiments were performed in phantoms with the photosensitizer Photofrin and in solution using phosphorescence-based singlet oxygen luminescence dosimetry (SOLD) to validate the SOED model. Oxygen concentration and photosensitizer photobleaching versus time were measured during PDT, along with direct SOLD measurements of singlet oxygen and triplet state lifetime (τA and τT), for various photosensitizer concentrations to determine necessary photophysical parameters. SOLD-determined cumulative [O2]rx was compared to SOED-calculated [O2]rx for various photosensitizer concentrations to show a clear correlation between the two methods. This illustrates that explicit dosimetry can be used when phosphorescence-based dosimetry is not feasible. Using SOED modeling, we have also shown evidence that SOLD-measured [O2]rx using a 523 nm pulsed laser can be used to correlate to singlet oxygen generated by a 630 nm laser during a clinical malignant pleural mesothelioma (MPM) PDT protocol by using a conversion formula.

Keywords: photodynamic therapy; singlet oxygen explicit dosimetry (SOED); singlet oxygen luminescence dosimetry (SOLD); Photofrin; oxygen

1. Introduction

Photodynamic therapy (PDT) is an evolving treatment modality for many cancers such as microinvasive lung cancer, obstructing lung cancer, and obstructing esophageal cancer, for premalignant diseases such as actinic keratosis, and non-oncologic conditions such as age-related macular degeneration [1–3]. PDT is advantageous for its low systemic toxicity, lack of induced resistance,
repeatability, and preservation of normal tissue structure. Widespread use of PDT has been restricted by the difficulty in accurately quantifying the effective treatment dose. PDT is dynamic and multifaceted, with complex and dynamic interactions between treatment light at a particular wavelength, photosensitizer (PS), and tissue oxygen ($[^3\text{O}_2]$) [3]. In a typical photodynamic process, the photosensitizer is excited by the treatment light and enters the excited singlet state. This singlet state undergoes intersystem crossing to the triplet state. This triplet state can react directly with molecular substrates or transfer a hydrogen atom or an electron to $[^3\text{O}_2]$ to produce radicals or radical ions in a type I process [4]. Most clinically relevant photosensitizers undergo type II processes in which the triplet state transfers energy to ground-state oxygen, $[^3\text{O}_2]$, to produce singlet oxygen, $[^1\text{O}_2]$ [4], which is the main photocytotoxic agent leading to cell death and therapeutic response [5,6].

PDT dosimetry has so far involved the prescription of an administered drug dose and a light fluence (energy per unit area). This is often inadequate due to the variation in photosensitizer localization from patient to patient as well as within the tumor environment [7,8]. Furthermore, tissue and blood oxygenation are key components for PDT and will affect not only the production of $[^1\text{O}_2]$ but also the tissue optical properties [9,10]. In turn, the penetration of light is dependent on the tissue optical properties [11]. Simplistically, PDT dose may be defined as the time integral of the photosensitizer concentration and the light fluence. However, this does not take into account the effect of tissue hypoxia. In a hypoxic environment, the production of $[^1\text{O}_2]$ will be lower than expected and treatment outcome will not be predictable [7,8].

For these compelling reasons, the use of singlet oxygen concentration, $[^1\text{O}_2]$ as the dosimetric measure has been suggested. Direct measurement of $[^1\text{O}_2]$ by its near-infrared luminescence emission is technically challenging in vivo due to the weakness of the signal and the short lifetime of $[^1\text{O}_2]$, ~30–180 ns [12,13]. Hence, a macroscopic singlet oxygen explicit dosimetry (SOED) model has been previously developed and studied for various sensitizers in vivo [8,14–16]. In the present work, SOED was compared in solutions to direct singlet oxygen luminescence dosimetry (SOLD) [17,18]. The relevant photophysical parameters for the macroscopic model were verified by performing explicit dosimetry of oxygen concentration and photosensitizer concentration. In performing a direct comparison between SOED- and SOLD-measured $[^1\text{O}_2]$, the use of SOED in scenarios where direct luminescence detection is difficult is validated. Furthermore, an analysis is provided to show that SOLD measured using a 523 nm pulsed laser (currently required by the availability of lasers with suitable pulse length, repetition frequency, and energy) is well-correlated to singlet oxygen generated by Photofrin by a CW 630 nm laser during PDT, by correcting for the tissue optical properties at the two wavelengths.

2. Materials and Methods

2.1. SOED Model In Vitro and In Vivo

Singlet oxygen produced during illumination was calculated using an explicit dosimetry model. Based on type II processes modeled, a set of coupled differential equations has been established for the photophysical reactions [8,16,19].

A set of simplified differential equations that are valid over time scales of a few seconds to hours can be used to describe the interactions of singlet oxygen concentration, $[^1\text{O}_2]$, photosensitizer concentration, $[S_0]$, the ground-state oxygen concentration, $[^3\text{O}_2]$, and the reacted singlet oxygen concentration, $[^1\text{O}_2]_{rx}$ for the in vitro scenario with parameters (and $k_i$) defined in Table 1 (and its footnote) [19]:

$$[^1\text{O}_2] = \xi \tau_\lambda \frac{[^3\text{O}_2]}{[^3\text{O}_2] + \beta [S_0]} \frac{1}{(\sigma([S_0] + \delta) + 1)}$$

$$\frac{d[S_0]}{dt} = -\frac{\xi}{[^3\text{O}_2] + \beta [S_0]} (\sigma([S_0] + \delta) \frac{\sigma([S_0] + \delta)}{(\sigma([S_0] + \delta) + 1)})$$
\[
\frac{d[^3\text{O}_2]}{dt} = -\frac{3}{[^3\text{O}_2] + \beta} \cdot \phi[S_0] \cdot \left( \frac{\sigma([S_0] + \delta) + k_7[A] \tau_\Delta}{(\sigma([S_0] + \delta) + 1)} \right)
\]
(3)

\[
[^1\text{O}_2]_{rx} = \int \frac{[^3\text{O}_2]}{[^3\text{O}_2] + \beta} \cdot \phi[S_0] \cdot \frac{1}{\sigma([S_0] + \delta) + 1} dt
\]
(4)

where \(\sigma = k_1/(k_6 + k_7[A])\), \(\zeta = \Phi_\Delta(\epsilon/\nu)\), \(\tau_\Delta^{-1} = k_6 + k_7[A]\), and \(\beta = k_4/k_2\). Here, \(\Phi_\Delta\) is the singlet oxygen quantum yield in the aqueous Intralipid medium. The parameters used for the calculation for each phantom are summarized in Table 1. For studies without NaN_3, the \(^1\text{O}_2\) quencher used in solutions, \([A] = 0\). For the in vivo scenario, Equations (2) and (3) can be rewritten as \([8,14–16,20]\):

\[
\frac{d[S_0]}{dt} = -\zeta \frac{[^3\text{O}_2]}{[^3\text{O}_2] + \beta} \cdot \phi[S_0] \cdot \sigma([S_0] + \delta)
\]
(5)

\[
\frac{d[^3\text{O}_2]}{dt} = -\left( \frac{\phi[S_0]}{[^3\text{O}_2] + \beta} \right) \cdot [^3\text{O}_2] + g \left( 1 - \frac{[^3\text{O}_2]}{[^3\text{O}_2]([t = 0])} \right)
\]
(6)

where we assumed that \(\sigma([S_0] + \delta) \ll 1\). Here we have added an oxygen perfusion term to account for vasculature in vivo, and the value of \(g = 0.7 \text{ } \mu\text{M/s}\) for Photofrin.

Equation (5) can be rewritten as the following:

\[
-\frac{d[S_0]}{dt} / \phi[S_0] \cdot \frac{[^3\text{O}_2]}{[^3\text{O}_2] + \beta} = \zeta \sigma([S_0] + \delta)
\]
(7)

The left-hand side of Equation (7) versus \([S_0](t)\) gives the values of \(\delta\) and \(\sigma\) used in Table 1. The photobleaching rate \((-d[S_0]/dt)\) was determined at each time point, along with the values of \(\phi\), \([^3\text{O}_2]\), \([S_0]\), and \(\beta\) for the calculation of the left-hand side of Equation (7). A linear fit to the data yields a value for the intercept and slope, and the intercept divided by the slope gives \(\delta\) and the slope divided by \(\zeta\) gives \(\sigma\). A recent review lists known values for in vivo photophysical parameters for many photosensitizers used clinically \([19]\). The SOED-calculated solutions were compared with the oxygen and \([S_0](t)\) concentrations. All calculations were performed using Matlab 2014b (MathWorks, Natick, MA, USA).

2.2. SOLD Instrumentation

Singlet oxygen luminescence dosimetry (SOLD) was performed using a compact, fiberoptic near-infrared probe-based system \([21,22]\). The probe was coupled to a compact InGaAs/InP single photon avalanche diode (SPAD) detector (Micro Photon Devices, Bolzano Italy). Samples were illuminated with a 523 nm wavelength pulsed laser (QL-523-200-S, CrystaLaser, Reno, NV, USA) coupled into the delivery fiber via a collimation package. Patterned time gating was used to limit the unwanted dark counts and eliminate the strong photosensitizer luminescence background. The luminescence signal from singlet oxygen at 1270 nm was confirmed through spectral filtering and lifetime fitting for Photofrin.

Figure 1 shows a photograph and schematic of the experimental setup. The pulsed laser was coupled into the delivery fiber. The laser also outputs an electrical signal that is sent to a programmable pulse pattern generator (PPG) (Agilent 81110A, Keysight Technologies, Inc., Santa Rosa, CA, USA). Each pulse generates outputs on two separate channels, each with pulse shape designed to match the intended input. The first output is a single pulse sent to the “start” channel of the time-correlated single-photon counting (TCSPC) module (HydraHarp, PicoQuant GmbH, Berlin, Germany), while the second is a pattern of pulses sent to the SPAD control module. The SPAD is turned on for a preassigned time, only when the control module receives a pulse from the PPG.
Figure 1. Singlet oxygen luminescence dosimetry (SOLD) instrumentation setup (a) on an optical bench; and (b) schematic diagram of the experimental arrangement. PPG—pulse pattern generator; SPAD—single photon avalanche diode; TCSPC—time-correlated single-photon counting.

The TCSPC module generates a timing histogram of photon counts versus time. The background was removed by subtracting the histogram taken through a 1210 nm filter from that through the 1270 nm filter. Equation (8) describes the $[\text{O}_2]$ signal as a function of time following a short illumination pulse.

$$[\text{O}_2](t) = N\sigma_A[S_0]\Phi_A\frac{\tau_A}{\tau_R - \tau_A}(e^{-t/\tau_A} - e^{-t/\tau_R})$$

Equation (8)

The cumulative SOLD singlet oxygen count can be calculated as the integral of Equation (8) per $\tau_R$ [23].

$$\int_0^\infty \frac{1}{\tau_R}[\text{O}_2](t)dt = \frac{N\sigma_A[S_0]\Phi_A\tau_A}{\tau_R}$$

Equation (9)

where $N$ is the number of photons in the illumination pulse, $\sigma_A$ is the PS absorption cross-section ($\sigma_A = (\epsilon/N_A) \times 10^9$), $N_A$ is Avogadro’s constant ($6.022 \times 10^{23}$), $\epsilon$ is the extinction coefficient, and $\tau_R$ is the $^3\text{O}_2$ phosphorescence lifetime ($k_0^{-1}$). A fit of the background-subtracted histograms was performed to Equation (8) (with a $y$-axis offset as a free parameter to account for any change in the background level) using Origin software with a Levenberg–Marquardt algorithm to iterate the parameter values.
2.3. Measurements in Tissue-Simulating Phantoms

Explicit dosimetry of phantom studies was performed using tissue-simulating liquid phantoms. A lipoprotein colloidal suspension, Intralipid (Fresenius Kabi, Uppsala, Sweden) was added to solutions to provide optical scattering. A broad beam (0.4 cm radius) was produced by a fiber with a microlens attachment (Pioneer Optics Company, Bloomfield, CT, USA) onto the side of cuvette phantoms. Oxygen measurements were made with a bare-fiber OxyLite probe (Oxford Optronix, Oxford, UK) on the side closest to beam entry at the center of the field. In the in vitro setup, there is very little oxygen diffusion at the point of measurement, so that oxygen measurements were performed with brief interruptions of the excitation laser at 1–30 s intervals. The oxygen partial pressure was measured in mmHg and converted to µM by using a factor of $\alpha = 1.3$ [14,24]. PS concentration was determined by obtaining fluorescence spectra produced by Photofrin excited by the treatment light. Spectral analysis was performed using single value decomposition fitting of the characteristic Photofrin peak [25].

2.4. Comparison of 630 nm and 523 nm SOED

Optical properties from multiple sites of several different patients undergoing treatment for pleural-PDT were determined from absorption spectra using a white light source (Avantes, Little Rock, AK, USA) connected to a multifiber contact probe, as described elsewhere [26,27]. The multifiber probe has a source fiber attached to a halogen white light source. This was used to obtain broadband reflectance at multiple source-detector separations. The diffusion equation was used to determine the solution for diffuse reflectance for a semi-infinite medium with steady-state excitation. The longitudinal distribution of $\phi$ for different tissue optical properties was determined using an analytical formula [28] based on Monte Carlo simulations [29–32]. To obtain the corresponding temporal changes of $[S_0]$ and $[^1O_2]$, the information of $\phi$ distribution, the magnitude of the Photofrin-specific reaction-rate parameters, and the measured photosensitizer concentrations [33] were passed to the time ($t$)-dependent differential Equations (5) and (6) for a given treatment time point, which were then used to calculate $[^1O_2]_{rx}$ using Equation (4).

3. Results

3.1. SOED Photophysical Parameters

Photophysical parameter values for Photofrin were determined for in vitro macroscopic modeling from the literature as well as measurements to be used in the calculation of $[^1O_2]_{rx}$. These parameters are listed in Table 1. Figure 2 shows the SOLD measurement of singlet oxygen lifetime as a function of the concentration of added sodium azide (NaNO$_3$), which is a potent singlet oxygen-specific quencher, for Photofrin in MeOH solution. The intercept of the linear fit (solid line in Figure 2) corresponds to $k_6$ and the slope corresponds to the value for $k_7$. 
Table 1. Summary of photophysical parameters for Photofrin in vitro and in vivo.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Definition</th>
<th>In Vitro</th>
<th>In Vivo</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\varepsilon$ (cm$^{-1}$·µM$^{-1}$)</td>
<td>Photosensitizer extinction coefficient</td>
<td>0.0035 at 632 nm (1)</td>
<td>0.0089 at 523 nm (1)</td>
</tr>
<tr>
<td>$\beta$ (µM)</td>
<td>Oxygen-quenching threshold concentration $\frac{1}{\delta}$ *</td>
<td>11.9 [34]</td>
<td></td>
</tr>
<tr>
<td>$\delta$ (µM)</td>
<td>Low-concentration correction</td>
<td>25 ± 4.3 (2)</td>
<td>33 [15]</td>
</tr>
<tr>
<td>$\xi$ (cm$^2$·mW$^{-1}$·s$^{-1}$)</td>
<td>Specific oxygen consumption rate $\xi = \frac{\Phi_A \lambda}{h\nu}$</td>
<td>$10.3 \times 10^{-3}$ (3) at 632 nm</td>
<td>$3.7 \times 10^{-3}$ [34] at 632 nm</td>
</tr>
<tr>
<td></td>
<td></td>
<td>24.8 $\times 10^{-3}$ (4) at 523 nm</td>
<td>8.99 $\times 10^{-3}$ (3) at 523 nm</td>
</tr>
<tr>
<td>$\sigma$ (µM$^{-1}$)</td>
<td>Specific photobleaching ratio where $\sigma = k_1 \tau_{\Delta}$ *</td>
<td>(6.6 ± 7) $\times 10^{-5}$ (2)</td>
<td>7.6 $\times 10^{-5}$ [8,34]</td>
</tr>
<tr>
<td>$\tau_{\Delta}$ (s)</td>
<td>Singlet oxygen lifetime $\frac{1}{k_4 + k_5[\text{O}_2]}$ *</td>
<td>(9.4 ± 0.2) $\times 10^{-6}$ (6)</td>
<td>1.6 $\times 10^{-7}$ [35]</td>
</tr>
<tr>
<td>$\tau_t$ (s)</td>
<td>Triplet state lifetime $\frac{1}{k_4 + k_5[\text{O}_2]}$ *</td>
<td>(0.43 ± 0.03) $\times 10^{-6}$ (7)</td>
<td>1.5 $\times 10^{-6}$ (7)</td>
</tr>
<tr>
<td>$\Phi_\Delta$</td>
<td>Single oxygen quantum yield</td>
<td>0.56 [36,37]</td>
<td>0.20 [19]</td>
</tr>
</tbody>
</table>

(1) Measured from absorption spectroscopy; (2) Obtained from fitting shown in Figure 3c using Equation (7); (3) Calculated using $\Phi_A = 0.56$ in water, $\varepsilon = 0.0035$ cm$^{-1}$·µM$^{-1}$, and $h\nu = 3.2 \times 10^{-16}$ mWs at 632 nm; (4) Calculated using $\Phi_A = 0.64$ in MeOH, $\varepsilon = 0.0089$ cm$^{-1}$·µM$^{-1}$, and $h\nu = 3.8 \times 10^{-16}$ mWs at 523 nm; (5) Scaled in vivo value at 632 nm by $\varepsilon$ at 523 nm$/\varepsilon$ at 632 nm; (6) Measured values from sold experiment when $[\text{O}_2] = 0$ (i.e., without NaN$_3$ in MeOH solution); (7) Calculated from measured data using $[\text{O}_2] = 40$ µM for in vivo conditions and $[\text{O}_2] = 169$ µM for in vitro conditions. Thereby, $\tau_t$ in vivo was estimated by determining $k_2$ in vitro ($1.3 \times 10^6$ µM$^{-1}$·s$^{-1}$) and using $\beta = k_4/k_2 = 11.9$ µM and $1/\tau_t = k_4[\text{O}_2] + k_5$; * The definition of the photophysical parameters are [19]: $k_1$ = rate of photosensitizer (PS) photobleaching; $k_2$ = rate of triplet PS quenching by $^3$O$_2$; $k_4$ = decay rate of triplet PS without $^3$O$_2$; $k_6$ = rate of $^1$O$_2$ phosphorescence decay; $k_7$ = rate of $^3$O$_2$ quenching by substrate.

![Figure 2](image-url) Singlet oxygen lifetime ($\tau_{\Delta}$) changes due to quenching with various concentrations of sodium azide (NaN$_3$) for Photofrin (50 µM) in MeOH, $\tau_{\Delta}^{-1} = k_6 + k_7[A]$. Symbols represent measured data and the solid line is the best linear fit.

3.2. SOED in Phantom

Photofrin phantoms with Intralipid as optical scatterer and absorption due to both the photosensitizer and water (or Intralipid) were used to measure the time dependence of $[^3\text{O}_2]$ and PS concentration, $[S_0]$, under CW 630 nm laser excitation. $[^3\text{O}_2](t)$ was measured using an oxygen phosphorescence probe and the photophysical parameters taken from Table 1.

Figure 3a,b show the measured $[^3\text{O}_2]$ and $[S_0]$ at just below the surface ($d = 0$) versus time in an Intralipid phantom (with $\mu'_s = 0.2$ cm$^{-1}$) for three different initial Photofrin concentrations (27, 50,
167 mM). The symbols are measured values and the lines are SOED-calculated results. Figure 3c shows the PS photobleaching rate per PDT dose, \( \frac{d[S_0]}{dt} = \frac{1}{[S_0][\Phi]_0/[1^{1}O_2]_0 + \beta \cdot t} \) versus \([S_0]_i\). The symbols are calculated values using Equation (7), and the line is the best linear fit. Figure 3d shows the expected SOED-calculated cumulative reacted singlet oxygen concentration, \([1^{1}O_2]_{rx}\), during illumination.

![Figure 3](image-url)

**Figure 3.** Comparison of measured and singlet oxygen explicit dosimetry (SOED)-calculated values of (a) \([1^{1}O_2](t)\) and (b) \([S_0](t)\) at \(d = 0\) for three initial photosensitizer concentrations, \([S_0]_i = 27, 50, 167 \mu M\). Measurements of ground-state oxygen were made at 5–30 s intervals, while photosensitizer spectra were obtained every 10 s. The average initial \([1^{1}O_2]_i\) value was 160.4 \mu M. (c) The left-hand side of Equation (7) versus the Photofrin concentration, with the line of best fit. The slope of the fit was 
\((6.86 \pm 0.6) \times 10^{-7} \text{mM} \cdot \text{s}^{-1} \cdot \text{mW}^{-1} \cdot \text{cm}^2\) and the intercept was \((1.78 \pm 0.25) \times 10^{-5} \text{mW}^{-1} \cdot \text{cm}^2\), resulting in a value of \(\delta = 25 \pm 4.3 \mu M\). (d) Calculated volume-averaged \([1^{1}O_2]_{rx}\) over time. The light fluence rates used in the experiment were \(\Phi_0 = 45, 38,\) and 42 mW/cm\(^2\) for each sensitizer concentration. The symbols are measured values in Figure 3a,b and are calculated values using Equation (7) for Figure 3c. The lines are SOED-calculated results for Figure 3a,b,d, and the line of best fit for Figure 3c.

### 3.3. SOED/SOLD Comparison in Solution

The singlet oxygen generated in Photofrin-containing solutions was calculated using SOED and the results were compared to SOLD-determined luminescence counts of \(1^{1}O_2\). The latter was correlated with the amount of \(1^{1}O_2\) produced instantaneously and cumulatively. Instantaneous \([1^{1}O_2]\) accounts for the singlet oxygen generated for each pulse of laser excitation, while cumulative \([1^{1}O_2]_{rx}\) is the integral of all singlet oxygen produced during the entire illumination time over the entire illumination volume. The agreement between the two methods (SOED and SOLD) is shown in Figure 4: (a) shows SOLD counts per accumulation time (in seconds, \(t = 300\) s before and after PDT) and (b) shows cumulative SOLD counts over the entire treatment time of 900 s. Photofrin was dissolved in MeOH solution.
were obtained using the SOLD system. Varying amounts of the singlet oxygen quencher, sodium azide (NaN₃) respectively, at 523 nm.

Figure 4. (a) Comparison of SOLD-obtained ¹O₂ counts (Equation (8)) per accumulation time (in seconds) at 523 nm and SOED-calculated instantaneous [¹O₂] (Equation (1)) for Photofrin concentrations in MeOH of 17, 50, and 83 μM, and light fluence φ₀ = 30 mW/cm². The initial oxygen concentration was measured as 175 ± 6 μM. (b) Comparison of SOLD cumulative ¹O₂ counts (Equation (9)) and reacted singlet oxygen concentration ([¹O₂]rx) calculated with SOED (Equation (4)) for Photofrin concentration of 17, 50, and 83 μM. PDT was performed with 523 nm light at φ₀ = 30 mW/cm² for 900 s.

4. Discussion

4.1. SOED and SOLD Intercomparison

The SOED calculated [¹O₂] value in solution in Figure 4a corresponded to the volumetric averaged instantaneous singlet oxygen concentration over a volume of 1 cm depth and 1 cm² area. SOED-calculated [¹O₂]rx in Figure 4b corresponded to the volumetric average reacted singlet oxygen concentration of the same 1 cm³ volume. In these solutions, the light fluence was calculated by introducing attenuation that was only due to the photosensitizer absorption, since no scatterer was added and solutions were of pure Photofrin: φ = φ₀ exp(−μₐ × d), where φ₀ is the light fluence rate (mW/cm²) measured directly in the back of the front wall of the solution facing the laser. Absorption coefficients (μₐ) were 0.15, 0.45, and 0.74 cm⁻¹ for Photofrin concentrations of 17, 50, and 83 mM, respectively, at 523 nm.

In order to experimentally determine the photophysical parameters of the spontaneous phosphorescence rate of ¹O₂ to ³O₂ (k₆) and the bimolecular reaction rate of ¹O₂ with the substrate (k₇) in Photofrin phantoms, photosensitizer triplet-state and singlet oxygen lifetime measurements were obtained using the SOLD system. Varying amounts of the singlet oxygen quencher, sodium azide (NaN₃), were added to the Photofrin–MeOH solutions. The resulting fits to obtain k₆ and k₇ are shown in Figure 2. For Photofrin with NaN₃, k₆ was found to be 1.14 × 10⁵ s⁻¹ (the intercept of the line of best fit in Figure 2) and k₇ was found to be 235 μM⁻¹s⁻¹ (the slope of the line of best fit in Figure 2). k₇ is pH-dependent, but is in the range of the reported value of 300–400 μM⁻¹s⁻¹ for the quenching rate constant in water [38]. These values were used to calculate τ₀ for the in vitro condition (without NaN₃) and the in vivo condition (taken from the literature for biological tissue [34]). Assuming that k₇ for NaN₃ is greater than or equal to that of in vivo conditions (assuming biological tissue is less efficient than NaN₃ in quenching ¹O₂), it can be estimated that in vivo acceptor concentration [A] ≥ 10⁷ (s⁻¹)/235 μM⁻¹s⁻¹ = 42 mM. This value is much higher than [A] = 0.83 mM in the literature [10], but we feel that it is more reasonable since the singlet oxygen lifetime in vivo, τ₀, does not change for reacted singlet oxygen concentrations [¹O₂]rx as high as 12 mM [16], indicating there are still plenty of acceptors in vivo at this level.
The light fluence rate distribution in a semi-infinite medium as a function of distance \(d\) was calculated by a Monte Carlo (MC) simulation [39] of a circular parallel beam (diameter 0.8 cm, Figure 5a) and broad beam (diameter 16 cm, Figure 5b) for absorption coefficient \(\mu_a\) of 0.09, 0.18, and 0.58 cm\(^{-1}\), and reduced scattering coefficient \(\mu_s'\) of 0.2 cm\(^{-1}\). The resulting \(\phi/\phi_0\) is shown in Figure 5 along with an exponential fit based on \(\mu_a\). For the tissue-simulating phantoms with Photofrin shown in Figure 3, \(\phi_0\) is the measured local fluence rate at the front inner surface of the phantom facing the laser and \(d\) is the depth from surface. At 630 nm, \(\mu_a = 0.09, 0.18, \) and 0.58 cm\(^{-1}\) for Photofrin concentrations of 27, 50, and 167 mM, respectively. It is clear that the function \(e^{-\mu_a d}\), while working well for the broad beam, does not work very well for the 0.8 cm diameter beam at the deepest depths investigated. As a result, MC-generated light fluence rate \(\phi/\phi_0\) was used directly for the SOED calculations in phantom.

SOED calculations of singlet oxygen concentration are highly dependent on the photophysical parameters used as input (Table 1). In turn, these parameters depend on the photosensitizer used, as well as the treatment environment. The necessary parameters for Photofrin-mediated PDT for in vitro studies were validated with explicit measurements of the \(^1\)O\(_2\) and \([S_0]\). In particular, the consumption rate of \([S_0]\) per PDT dose was used to determine a more accurate value of \(\sigma\) (slope/\(\xi\)) and \(\delta\) (intercept/slope) for the experimental setup used (Figure 3c and Equation (7)). This was used to determine \(\delta\) and \(\sigma\) using a method from Reference [40] that is also described in Section 2.1. Photosensitizer concentration was measured over time to determine the photobleaching rate \((-d[S_0]/dt)\) and \([S_0]\). Along with the measured \(^1\)O\(_2\), the PS photobleaching rate per PDT dose can be calculated and plotted as in Figure 3c. The slope and intercept of the fit to the data are used to calculate \(\delta\) and \(\sigma\). The value for \(\xi\) in vitro was calculated by the definition of \(\xi\) provided in Table 1. The resulting values were \(\delta = 25 \pm 4.3\) μM and \(\sigma = (6.6 \pm 7) \times 10^{-5}\) μM\(^{-1}\). The value of \(\beta\) was set to be 11.9 μM for this set of experiments [34]. Figure 3a,b show the SOED calculations using Equations (2) and (3), which agree with \(^1\)O\(_2\)[\(t\)] and \([S_0]\)[\(t\)] measurements at surface \((d = 0\) cm\) of the Intralipid phantom. Figure 3d shows the magnitude of SOED-calculated \(^1\)O\(_2\)\(_{rx}\) using Equation (4) for Photofrin to be in the mM range.

![Figure 5. Monte Carlo (MC) simulation of fluence rate distribution by a circular beam of radius (a) 0.4 cm and (b) 8 cm incident on a semi-infinite liquid surface as a function of depth \(d\) for \(\mu_a = 0.09, 0.18, \) and 0.58 cm\(^{-1}\) and \(\mu_s' = 0.2\) cm\(^{-1}\). Fits of exponential forms are shown along with the MC data. The exponential form of \(e^{-\mu_a d}\) fits the simulation well up to a depth of 0.4 cm, while overestimating \(\phi/\phi_0\) at larger depths. Broad-beam simulations agree with the simple exponential form up to a depth of 1.3 cm.](image-url)
It can be concluded from the intercomparison of SOED and SOLD in Photofrin solutions (Figure 5b) that the cumulative SOLD $[^1O_2]$ counts, [SOLD], and SOED-calculated $[^1O_2]_{rx}$ values track each other very well ($R^2 = 0.98$) for Photofrin, with a conversion factor of the following form:

$$[^1O_2]_{rx}(mM) = \left(2.16 \times 10^{-5}\right) \times [SOLD] - 11.8$$

(10)

The ratio of slopes between the two panels ((a) and (b)) in Figure 4 is $9.6 \times 10^{-6}$ s, which is consistent with the value of $\tau_\Delta$ obtained (9.4 $\times 10^{-6}$ s). The reason for the intercept is not known, and a linear fit without intercept reduces the correlation ($R^2 = 0.86$). The good correlation of SOED-calculated $[^1O_2]$ and [SOLD] demonstrates that SOED can be utilized in scenarios where direct phosphorescence measurement of $[^1O_2]$ is difficult.

4.2. Feasibility of Using SOLD at 523 nm for Predicting $[^1O_2]_{rx}$ at 630 nm

Currently, the only available pulsed laser suitable for the SOLD application (CrystaLaser, QL-523-200-S, CrystaLaser, Reno, NV, USA) is at 523 nm. As a result, the effective tissue-sampling depth for $[^1O_2]$ is not the same as that of the 630 nm treatment light used clinically with Photofrin. Figure 6 shows the measured values $\mu_a$ and $\mu_s'$ in various sites measured in vivo in patients, including the anterior chest wall, apex of the heart (apex), posterior chest wall, diaphragm (diaph), serratus (ser), anterior sulcus, posterior sulcus, pericardium (peri), and normal (norm) tissue. Patients were undergoing an institutional review board (IRB)-approved pleurodesis Photofrin-PDT clinical protocol at the University of Pennsylvania. These optical properties were measured using a custom-built multifiber contact probe for absorption spectroscopy [27]. The measured optical properties include $\mu_a$ and $\mu_s'$ for tissue as well as Photofrin.

![Figure 6](Figure 6. (a) Tissue $\mu_a$ and (b) $\mu_s'$ at 523 (hollow symbols) and 630 (filled symbols) nm measured in vivo in malignant pleural mesothelioma (MPM) patients.)

Using an analytical fit [28] to MC simulations [29–32], the longitudinal distribution of $\phi$ in tissue with different optical properties was calculated. Figure 7 shows the ratio of $\phi$ and in-air fluence rate ($\phi_{air}$) versus tumor depth for (a) 523 nm and (b) 630 nm. The gray area shows the region of $\phi/\phi_{air}$ with the upper and lower bounds of the tissue optical properties obtained in vivo as dark blue and light blue, respectively. The dashed black lines show the calculated light fluence distribution using the mean optical properties of $\mu_a = 5.52 \text{ cm}^{-1}$ and $\mu_s' = 17.61 \text{ cm}^{-1}$ for 523 nm and $\mu_a = 0.58 \text{ cm}^{-1}$ and $\mu_s' = 15.61 \text{ cm}^{-1}$ for 630 nm. As expected, the optical penetration is much deeper at 630 nm than at 523 nm in in vivo malignant pleural mesothelioma (MPM) patients.
where the PS concentration (in µM) and φ is the light fluence (in J/cm²). We thus conclude that SOLD measurement at 532 nm can be used to monitor [¹⁰O₂]rx at 630 nm if a conversion formula (Equations (11)–(13)) is used to convert the measured SOLD signal.

When SOLD signal from patients are used to determine the generation of singlet oxygen, it is important to develop a tissue optical properties correction factor to account for the absorption and scattering of luminescence by tissue, similar to the optical properties correction factor needed for using fluorescence to determine the PS concentration [14]. This is beyond the scope of this paper.

The φ distributions were then used to calculate the reacted singlet oxygen concentration for the two wavelengths, in order to study whether SOLD signals measured at 532 nm can be used to monitor [¹⁰O₂]rx at 630 nm. MPM PDT is currently performed at 630 nm. Correlation between the calculated [¹⁰O₂]rx for 630 and 523 nm is shown in Figure 8. μa ranges from 0.66 to 23.1 cm⁻¹ at 523 nm and 0.17 to 1.35 cm⁻¹ at 630 nm, while μs' ranges from 2.80 to 73.7 cm⁻¹ at 523 nm and 2.55 to 30.5 cm⁻¹ at 630 nm (Figure 6). In order to investigate the effects of different φ on the [¹⁰O₂]rx, the SOED calculations were repeated for φ = 5, 25, 50, 75, and 150 mW/cm². Different colors of symbols represent different φ. The black solid lines are the best fits in Figure 8b. At 523 nm, the range of [¹⁰O₂]rx changed from 0–0.1, 0–0.63, and 0–5.6 mM for PS concentrations of 0.21, 2.1, and 21 µM, respectively, while the range of [¹⁰O₂]rx at 630 nm changed from 0–0.25, 0–2.5, and 0–20 mM, respectively, for the same PS concentrations.

The resulting correspondence for a range of PS concentrations (c) of 0.21, 2.1, and 20.1 mM (based on the average Photofrin concentration obtained in patients) and light fluence of 10–120 J/cm² [33] can be expressed as:

\[ [¹⁰O₂]_{rx}(630 \text{ nm}) = a(c) [¹⁰O₂]_{rx}(523 \text{ nm}) + b(c, \phi) \]  (11)

where

\[ a(c) = 0.05814c + 1.922 \]  (12)

and

\[ b(c, \phi) = (0.000618c - 0.000033)\phi \]  (13)

Figure 7. The ratio of φ and in-air fluence rate (φair) versus tumor depth for (a) 523 nm and (b) 630 nm optically broad laser beams on an air–tissue interface using an analytical formula that fits MC simulation [29–32] and optical properties obtained in in vivo MPM patients (Figure 4).
assumptions. Furthermore, the validation of SOED must be carried out for each photosensitizer and set in applying SOED to ensure that the treatment parameters lie within the range of validity of these more robust in that no simplifying assumptions are required as in SOED. Hence, care must be taken in applying SOED to ensure that the treatment parameters lie within the range of validity of these assumptions. Furthermore, the validation of SOED must be carried out for each photosensitizer and set of clinical conditions. In the future, with developments such as our recent report of fiberoptic-coupled

\begin{align}
\kappa \text{O}_2 \cdot \phi & = \phi \text{O}_2 \cdot \phi
\end{align}

**Figure 8.** (a) $[^1]\text{O}_2\text{rx}$ calculated at 630 nm and 523 nm for different total fluence ($\phi = 10, 60, 120 \text{ J/cm}^2$) for mean Photofrin concentrations ($c$) of (from left to right) 0.21, 2.1, and 21 $\mu\text{M}$. Absorption and scattering coefficients were obtained at the two wavelengths from Figure 6. SOED calculation of $[^1]\text{O}_2\text{rx}$ used Equations (5) and (6) and averaged over a 1 cm depth and 1 cm$^3$ volume using photophysical parameters listed in Table 1 for the in vivo conditions; (b) Slope and intercept of the correlation of $[^1]\text{O}_2\text{rx}$ at 630 nm and 523 nm as a function of fluence and PS concentration.

5. Conclusions

Direct singlet oxygen luminescence dosimetry (SOLD) measurements were compared with singlet oxygen explicit dosimetry (SOED) calculations for phantoms using Photofrin. Oxygen and PS concentration measurements were compared with SOED predictions to validate the SOED model and to obtain the photophysical parameters (Table 1, $\delta = 25 \pm 4.3 \mu\text{M}$ and $\sigma = (6.6 \pm 7) \times 10^{-5} \mu\text{M}^{-1}$ in vitro). Using lifetime measurements obtained with the SOLD system, photophysical parameters $k_6 \,(1.14 \times 10^{-5} \text{ s}^{-1})$ and $k_7 \,(235 \mu\text{M}^{-1}\text{s}^{-1})$ were found for in vitro solutions with NaN$_3$. A linear relationship between SOLD singlet oxygen photon counts at 1270 nm and SOED-calculated reacted singlet oxygen (Equation (10)) was established for Photofrin for 523 nm light excitation. Based on our SOED calculations, a formula (Equations (11)–(13)) for converting cumulative SOLD signal measured at 523 nm to the corresponding $[^1]\text{O}_2\text{rx}$ at 630 nm was established using the optical properties at the two wavelengths in an ongoing MPM clinical protocol.

These results indicate that, with suitable correction for the tissue optical properties at the two wavelengths, there is excellent correlation between the direct (SOLD) and indirect (SOED) estimates of the singlet oxygen generated during PDT. Since, at the present time, the SOED approach is technically simpler and the instrumentation is significantly less expensive, this validation supports its use in clinical dosimetry. It should be noted, however, that the SOLD technique is intrinsically more robust in that no simplifying assumptions are required as in SOED. Hence, care must be taken in applying SOED to ensure that the treatment parameters lie within the range of validity of these assumptions. Furthermore, the validation of SOED must be carried out for each photosensitizer and set of clinical conditions. In the future, with developments such as our recent report of fiberoptic-coupled
SOLD techniques based on novel superconducting nanowire single-photon detector technologies of direct SOLD, which currently can be considered as the laboratory Gold Standard for PDT dosimetry, may accelerate movement towards clinical utilization of SOLD alongside SOED. For type I PDT with photosensitizers, where a reactive oxygen species (e.g., oxygen radicals) other than singlet oxygen is the main cytotoxic agent, it is still possible to model the photophysical process using SOED, as described in a recent review [19]. However, it remains a challenge to find the value of photophysical parameters needed to describe the type I interactions for those photosensitizers.

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Conflicts of Interest: The authors declare no conflict of interest.

Abbreviations
The following abbreviations are used in this manuscript:
PS Photosensitizer
SOED Singlet Oxygen Explicit Dosimetry
SOLD Singlet Oxygen Luminescence Dosimetry

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