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Simulation of the electrohydrodynamic instability process used in the fabrication of hierarchic and hollow micro/nanostructures

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This article demonstrates that the electrohydrodynamic patterning process, a novel technique for the manufacturing of micro- and nano-scale structures, also allows the one-step realization of hierarchical structures and hollow structures. Through numerical simulation, it is shown that multilevel structures can be obtained if process time and applied electric voltage are optimized. As an example, the growth of structures with a width of around 187 nm and depth of 95 nm has been successfully simulated alongside structures with a width of around 0.4 μm and depth of 0.8 μm. The width of the protrusive mask patterns is shown to determine whether hollow structures with single or multiple shapes can be formed using electric field assisted capillarity. The numerical simulation process effectively demonstrates that the realization of micro/nano-structures with hierarchic and multilevel shapes can be considered as an innovative manufacturing process for MEMS or micro/nanofluidic structures.

Introduction

Electrohydrodynamic instability patterning is a novel technique, which has potential applications for the economical and efficient manufacturing of micro- and nano-scale structures. This technology takes advantage of the Maxwell stress generated by two media of different dielectric constants subjected to an electric field, to induce the self-assembling micro/nanostuctures in one of the media. A number of studies on the electric induced destabilization mechanisms have been investigated for their usefulness in lithography. The spontaneous formation of periodical pillars with space equaling the most unstable wavelength induced by the electric field has been well characterised as well as its capability to generate three-dimensional structures even without the requirement of a patterned mask. The heterogeneous electric field generated by a patterned mask should be used however to realize precise control over the emerging pattern in the film. The patterned template induces a laterally varying electric field that has a two-fold influence on the development of the surface instability. Firstly, the instability is directed towards the template protrusions due to the pressure gradients induced by the height variations of the template. In addition, these protrusions generate a larger electric field strength that leads to a locally increased growth rate of the instability. As a consequence, a positive replica of the template structure is obtained. The generation of a modulated electric field can be implemented either by a patterned conducting surface, dielectric patterns on a conductive substrate or electrically conductive patterns on a dielectric substrate.

More recently, a method combining electrostatic field and capillarity effects was demonstrated to form hollow structures. The resulting Electrical Field Assisted Capillarity (EFAC) process, as an extension of the Electrohydrodynamic Induced Patterning (EHDIP) method, is a novel manufacture process of hollow microstructures. The notable difference of EFAC from EHDIP is that the top electrode is a heavily wetted, low surface energy surface, which subjects the polymer to a large capillary force when it reaches the surface of the top mask, thus enabling the rapid coating of the mask and the formation of a shell of a few microns thick. In this paper, we demonstrate that hierarchic or multilevel hollow structures can be obtained in one step by using a conductive patterning template on a dielectric substrate via electric field assisted capillarity.

In the past, a non-linear 3D model proposed by Verma et al. to simulate the EHDIP process revealed that patterns formed by a heterogeneous electric field were determined by the interplay of two lateral length scales that are intrinsic to this process. One length scale is the destabilization wavelength, which is determined by the balance of the destabilizing electrostatic pressure gradient and the restoring interfacial tension. The other length scale is the periodicity of the patterned master template. Therefore, it is necessary to study how to utilize the structured electric field to

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suppress the intrinsic characteristic wavelength corresponding to the first length scale mentioned before by optimizing the process parameters. Our previous work was devoted to answer the above-mentioned question. For many applications, however, it is desirable to control the spatial arrangement of more than one component. With traditional methods, this requires an iterative, multistep procedure, making the replication process more complex and less reliable. Electrohydrodynamic instability can produce a hierarchical lateral structure that exhibits two independent characteristic dimensions.

In this article, we aim to extend the application of EHDIP and EFAC in realizing micro/nano-structures with hierarchical and variable multilevel shapes. To further understand the fundamentals of EHDIP and EFAC process, theoretical models based on the finite element analysis simulation software COMSOL Multiphysics (version 4.3) have been developed in this paper. It is demonstrated that hierarchical structures and hollow structures can be realized in one step. For EHDIP, the influence of operational parameters such as the width and height of master electrode, electrodes spacing, the period of master electrode and initial film thickness has been studied in detail to realize the formation of hierarchical structures.

Presentation of the simulation model

Consider a viscous polymer film surrounded by air and resting on a planar substrate under the influence of a heterogeneous electric field, as shown in Fig. 1. Fig. 1(a) shows a conductive patterned electrode and planar substrate. Fig. 1(b) shows the conductive patterns on a dielectric substrate. For a patterned mask, the height of the electrode protrusions, the width of the electrode protrusions, and the period of the grating mask are denoted by \( p, w \) and \( l \), respectively. The master electrode applied with voltage \( u \) is positioned above the substrate at distance \( d \). The points A, B, and C in Fig. 1(a) are specified positions used to demonstrate the pressure jump in the film.

![Diagram of polymer film](image)

**Fig. 1.** Schematic diagrams of a polymer film resting on a planar substrate under the influence of a heterogeneous electric field. (a) presents the mask as a conductive patterned electrode. (b) shows the mask as a type of conductive pattern on a dielectric substrate.

**Numerical method**

In this work, the level set two-phase flow application and electrostatic modules in COMSOL Multiphysics are adopted to simulate EHDIP. The conservative level set method is an interface tracking method, which is used for computing multiphase flow problems. The interface between fluid (gas and liquid) is represented by the 0.5 contour value of the level set function \( \phi \) whose range is between 0 and 1. A smeared Heaviside function considers that \( \phi < 0.5 \) for one phase, \( \phi > 0.5 \) for the other and the transition is varied smoothly across the interface. The level set equation is expressed as:

\[
\frac{\partial \phi}{\partial t} + \mathbf{U} \cdot \nabla \phi = \frac{\gamma}{\eta} \left( \varepsilon \nabla \phi - \phi (1 - \phi) \nabla \phi \right)\]

where \( \gamma \) is the stabilization parameter; \( \varepsilon \) is the parameter that controls the interface thickness and should have the same order as the computational mesh size of the elements where the interface propagates; \( \mathbf{U} \) is the velocity vector of the interface, which can be solved by the Navier–Stokes (N–S) equations. The momentum equation,

\[
\rho \frac{\partial \mathbf{U}}{\partial t} + \rho (\mathbf{U} \cdot \nabla) \mathbf{U} = -\nabla p + \nabla \cdot (\mu \nabla \mathbf{U}) + \mathbf{F}
\]

and the continuity equation,

\[
\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{U}) = 0
\]

are the N–S equations, where \( \rho \) is the density, \( \mu \) is the viscosity and \( p \) is pressure. \( \mathbf{F} \) is the volume force caused by the atmospheric pressure \( p_0 \), the surface tension \( \mathbf{F}_d = \sigma \mathbf{n} \), and the electrostatic pressure \( p_d \), \( \mathbf{F} = (p_d + \sigma \mathbf{n}) \delta \mathbf{n} \), where \( \sigma \) is the surface tension coefficient (N m\(^{-1}\)), \( \kappa \) is the curvature, \( \delta \) is a delta function concentrated to the surface, and \( n \) is the unit outward normal to the interface. \( \delta \) smoothens the surface tension which is concentrated at the interface between fluids and is approximated according to the equation

\[
\delta = |\nabla \phi| \phi (1 - \phi)\]

The interface normal vector modulus and the interface curvature are determined by eqn (5) and (6) respectively.

\[
n = \frac{\nabla \phi}{|\nabla \phi|}\]

\[
\kappa = -\nabla \cdot \left( \frac{\nabla \phi}{|\nabla \phi|} \right)
\]

The density and viscosity are calculated from

\[
\rho = \rho_1 + (\rho_2 - \rho_1)\phi
\]

\[
\mu = \mu_1 + (\mu_2 - \mu_1)\phi
\]

where \( \rho_1 \) and \( \rho_2 \) are the fluid densities of the air and polymer film; \( \mu_1 \) and \( \mu_2 \) indicate the dynamic viscosities of the air and the polymer film. The electric field is solved using the Laplace's
equation for the voltage assuming that there is zero free charge in the bulk fluid:

\[ \nabla \cdot \nabla V = 0 \]  \hspace{1cm} (9)

The electrostatic pressure can be described by the following equation:\(^{17}\)

\[ p_{el} = -0.5 \varepsilon_0 \varepsilon_p (\varepsilon_p - 1) E_p^2 \]  \hspace{1cm} (10)

For convenience, the schematic diagrams of the EHDI process on planar substrate (Fig. 1(a) and (b)) are taken to show the geometry, boundary conditions and mesh of the two-dimensional model. In order to highlight versatility and exhibit the process evolution, only four periods of the pattern on master electrode are shown here. The geometry and mesh of the model are presented in Fig. 2. For a conductive patterned electrode, a DC voltage is applied between the bottom (boundary 2) and the top electrode with electrical potential (boundaries 5, 6, 7, …, 19, 20 and 21). For a partial conductive electrode, i.e. conductive pattern on a dielectric substrate, the boundary 5, 9, 13, 17 and 21 are set to be at zero potential; the other boundary conditions are similar to those of the conductive patterned electrode. The boundary conditions for the fluid flow are: (a) no slip at boundaries 2, 5, 6, 7, …, 19, 20 and 21; (b) periodic boundary on boundaries 1, 3, 22 and 23; (c) initial fluid interface at boundary 4. In order to simulate a periodic structure, it is necessary to introduce the periodic boundary conditions at boundaries 1, 3, 22 and 23. The sources 1 and 3 corresponding to the destinations 23 and 22, respectively. The expressions for the sources are the pressure in the fluid \( P \) and the flow velocity \( U \). Two-phase flow is in the form of conservative level set. Properties of the polymer liquid used in the simulation are presented in Table 1.

Results and discussions

The periodic pattern on the template generates a periodic electric field on the air–polymer interface, where the larger electric field intensity corresponds to the protrusion on the template, and the lower electric field intensity corresponds to the cavity. So the electrostatic force on the polymer–air interface is periodic considering that the electrostatic force is an almost square relation to the electric filed strength. This modulated electrostatic force attracts the polymer as it moves upwards to form structures similar to the patterns on the template.

Fig. 2 Schematic diagram introducing the geometry, boundary conditions and mesh of the two-dimension model. Dimension unit is \( \mu \text{m} \).

The detailed time evolution of the electrically induced patterning process with patterned conductive template is shown in Fig. 3. Simulation results show a two-dimensional periodic microstructure induced by a conductive patterned electrode with protrusion height of 0.2 \( \mu \text{m} \) and width of 0.2 \( \mu \text{m} \). The period \( f \) of the protrusion is 1 \( \mu \text{m} \). The gap \( d \) between the electrodes is 1 \( \mu \text{m} \). The initial polymeric film thickness is 0.3 \( \mu \text{m} \). The applied DC voltage on the top electrode is 500 \( \text{V} \) and the bottom electrode is grounded. Initially the polymer film surface is flat as shown in Fig. 3(A). As the spatial heterogeneity of the electrostatic field is introduced by the patterned top electrode, the polymer liquid grows upwards firstly under the protrusions of the top electrode due to the higher electric field in those areas as shown in Fig. 3(B). The resulting uplifted polymer experiences a greater electrostatic force as the polymer approaches the top electrode, pulling the polymer fluid further towards the protrusion of the top electrode. The growing polymer touches the surface of the top electrode, and is stopped from moving further upwards as indicated in Fig. 3(C). Since the larger electrostatic force difference emerges at the boundaries of the polymer columns, the polymer material at the boundaries is rapidly depleted, leaving residual polymer between the columns as shown in Fig. 3(D). As the process is developing, the residual polymer forms small humps, hence the multilevel structures can be obtained in one step as shown in Fig. 3(E). However these humps do disappear for a suitably long duration of the process such that the complete replica of the mold can be obtained with potentially a larger height-to-width aspect ratio. It is found that if the applied voltage is less than 500 \( \text{V} \), the intermediate evolution stages, shown in Fig. 3(D) and (E), do not appear. In this case, the hierarchical structures cannot be obtained. In this particular case, large structures with width of around 187 \( \text{nm} \) (full-width at half-maximum) and depth of 95 \( \text{nm} \) can be created concomitantly with structures of 400 \( \text{nm} \) width and 800 \( \text{nm} \) depth as shown in Fig. 3(E). In general, similar multilevel structures can be obtained for large applied voltage values and moderately short process times.

The mechanism behind the flow phenomenon shown in Fig. 3 is the uneven pressure distribution in the film. Fig. 4 shows how the pressure distribution and velocity values change during the process. The spatial heterogeneity of the electrostatic field induces the uneven pressure distribution on the film surface. The pressure difference between point A and C is about 7.6 \( 10^{5} \) \( \text{Pa} \) induces the transverse flow. The pressure difference becomes larger during the columns formation and is about 8.74 \( 10^{5} \) \( \text{Pa} \) between points A and C as shown in Fig. 4(B). In the Fig. 4(B), the pressure difference between point A and B reaches to 1.24 \( 10^{6} \) \( \text{Pa} \), but the pressure difference between points B and C is just 0.31 \( 10^{6} \) \( \text{Pa} \), therefore the larger pressure gradient between A and B leads to more fluid flowing to the corner area. As a result, the polymer material at point B is depleted as shown in Fig. 4(D). Finally, hierarchical structures form in the polymeric film as shown in Fig. 4(E).

Fig. 5 shows the diagram of polymer film and the electric field strength distribution at the film surface at the initial stage. The electric field distribution follows a sinusoidal profile. The electric field strength underneath the center of the protrusion is...
much larger than in the other areas, such that a larger electrostatic force is exerted on the film surface. Accordingly, the internal pressure at this point is higher than in the other areas.

Furthermore, we have studied in detail how the change of process parameters, such as electrode geometries \((d, l, w, p)\) as well as polymer layer thickness affect the formation of the hierarchical structures based on the results in Fig. 3. Fig. 6 shows the changing trend of the hierarchical structures under different widths of electrode protrusions \(w\). It can be clearly seen that the hierarchical structures can be obtained without considering the change of the width of electrode protrusions.
However, the change of the width of the electrode protrusions influences the heights of small humps, the maximum height of the hump is obtained for the width of the electrode protrusions reaching 0.5 μm, meaning filling factor (w/l) is 0.5. In general, the change of the width of the electrode protrusion w does not affect largely the formation of the hierarchical structures.

Fig. 7 shows the variation of hierarchical structures against the electrode spacing d. The hierarchical structures can be obtained with the smaller electrode spacing d in Fig. 7(A), with the increase of the electrode spacing, the height of the small humps decreases as shown in Fig. 7(B), in extreme cases, no small humps are presented as in Fig. 7(C). In general, the increase of the electrode spacing d was unfavourable for the formation of the hierarchical structures.

Fig. 8 shows how the changes of the film thickness affect the formation of the hierarchical structures. The largest height of the small humps can be obtained when the film thickness is minimal as shown in Fig. 8(A); no hierarchical structures were present when the film thickness is larger as in Fig. 8(C). In general, the increase of the film thickness will largely go against for the formation of the hierarchical structures.

Fig. 9 shows how the changes of the distance of the electrode protrusions (i.e. the period l) influence the formation of the hierarchical structures. The largest height of the small humps can be obtained when the distance of electrode protrusions is maximum as shown in Fig. 9(C); no hierarchical structures were present when the distance of the electrode protrusions is small as in Fig. 9(A). In general, the increase of the distance of the electrode protrusions will certainly help the formation of the hierarchical structures.

Fig. 10 shows how the changes of the different height of the electrode protrusions influence the formation of the hierarchical structures. The largest height of the small humps can be obtained when the height of the electrode protrusions is minimum as shown in Fig. 10(A); the independent structure of columns underneath the protrusions appears with no formation of the small humps as in Fig. 10(C). In general, the decrease of the height of the electrode protrusions is beneficial to the formation of the hierarchical structures.

Fig. 11 shows the simulation results of multilevel periodic hollow microstructures induced by the conductive pattern on a dielectric substrate via electric field assisted capillarity. Here the electrode protrusion is 0.2 μm high and 1 μm wide. The gap d between the protrusions is 1 μm, the period l is 2 μm, and the initial film thickness is 0.68 μm with a 0.12 μm gap between the film surface and lowest part of the electrode. The applied DC voltage is 420 V.

The process starts in the same way with a thin polymer film between two electrodes as shown in Fig. 11(A). Due to the high contrast of the electrostatic force at the corner of the electrode protrusions and as long as the width of the protrusion is relatively large, the periodic concave structures emerge at the surface of the
polymer as presented in Fig. 11(B). The process differs from EHDIP when the polymer reaches the top mask as shown in Fig. 11(C). Since the top mask is hydrophilic, the capillary force will drive the polymeric liquid flow along the surface of the top electrode as indicated in Fig. 11(D). As a result, the flow of the fluid will meet at the middle point of the protrusions as well as the middle point of the gap between protrusions as shown in Fig. 11(E). Finally, the multilevel hollow structures can be formed in the polymeric film, Fig. 11(F). The diameter of the small hollow structures is 36 nm. However, if the aspect ratio of height to width of the electrode protrusions is increased, only hollow structures under the cavity can be obtained. As a result, the width of the protruding mask pattern is critical to determine if single or multiple hollow structures can be formed by the EFAC process.

Fig. 11 Spatiotemporal evolution of multiple hollow structures for 0.68 μm initial film thickness. Red color represents the polymer liquid, and the blue represents air.

Fig. 12 Evolution of the pressure (color) and velocity (black arrows) at various time steps for the case shown in Fig. 11. The pressure unit is Pa and the velocity unit is m s⁻¹.

to Fig. 11. Initially there is a pressure jump of around $7.51 \times 10^5$ Pa in the film underneath the corners of the protrusion. The jump is caused by the heterogeneous electric field shown in Fig. 13. In the whole process, the pressure inside the hollow structures is larger than that in the surrounding polymeric fluid and the pressure jump is maximal at the bottom of the hollow structures, so the hollow structures moves down.

In the process of forming hollow structures, the diagram of polymer film and the electric field strength distribution on the film surface at the initial stage is showed in Fig. 13. The much larger strength of electric field underneath the corners of the protrusions leads to the larger gradient of the electrostatic force at the corners, which induces instability of the film at these points first.

Fig. 13 Electrically induced hollow structures for a patterned template. (A) Diagram of polymer film at initial time, the red line together with the blue line is the shape of the protrusions of the master electrode with electrically conductive patterns (the blue line) on a dielectric substrate (the red line) and the green line is the air–polymer interface. (B) Initial electric field distribution on the film surface for the case of hollow structures shown in Fig. 11. The dotted line is used to characterize the largest electric field strength located at the surface of the polymer film.
Fig. 14 shows the simulation results of both sealed hollow microstructures and non-sealed open microstructures induced by the conductive pattern on a dielectric substrate via electric field assisted capillarity. Here the electrode protrusion is 0.2 μm high and 1 μm wide. The gap d between the protrusions is 1 μm, the period l is 3 μm, and the initial film thickness is 0.65 μm with a 0.15 μm gap between the film surface and lowest part of the electrode. The applied DC voltage is 420 V.

Conclusions

In summary, we have demonstrated through simulations that multilevel structures can be obtained by the proper control of EHDIP process parameters. It is found that smaller initial film thickness, smaller electrode spacing and larger distance of the electrode protrusions help to achieve the hierarchical structures. Furthermore, it is found that a proper width of the electrode protrusion and smaller height of the electrode protrusion are helpful to achieve hierarchical structures. Moreover, it is found that the electric field assisted capillarity can create hierarchical hollow structures using a patterned master electrode. Numerical computing results show that hollow structures with diameter of 36 nm can be achieved. The structures with both sealed hollow structures and non-sealed open structures co-existing can be obtained. Our results shed some light on the mechanisms by which multiple patterns in the form of hierarchical structures or hollow structures can be formed in the film. These unique structures have potential applications in MEMS or micro/nanofluidics.

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