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Spontaneous polarization of solid CO on water ices and some astrophysical implications

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Reflection Absorption Infrared Spectroscopy (RAIRS) is used to show that when 20 monolayer (ML) films of solid CO are laid down on solid water substrates at 20 to 24 K, the films polarize spontaneously. CO films were prepared on three types of water ice: porous amorphous solid water (CO-pASW), crystalline water (CO-CSW) and compact amorphous solid water (CO-cASW) with corresponding fields of 3.76±0.15 x 10^7 V m^-1 for CO-pASW, 2.87±0.15 x 10^7 V m^-1 for CO-CSW and 1.98±0.15 x 10^7 V m^-1 for CO-cASW. For comparison, CO laid down on SiO2 yields 3.8±0.15 x 10^7 V m^-1. Our results are of relevance to an understanding of the chemistry and physics of dense star-forming regions in the interstellar medium, in which dust particles become coated with solid CO on a layer of cASW. The polarization charge which accumulates on the CO surface acts as a catalyst for the removal of electrons and ions from the medium and may account for the low degree of ionization observed in these regions, a feature which is an important factor for the rate of star formation.

1. Introduction

Previous work has shown that when a dipolar molecular gas is condensed onto a cold substrate, a solid film may be formed which spontaneously exhibits a static electric field\(^1,2,3,4,5,6,7,8,9\), the strength of which may exceed \(10^7\) V m\(^{-1}\). Such solid films are referred to as spontlectric, an elision of ‘spontaneously electrical’. Spontlectric materials discovered to date all possess a permanent dipole moment and range over CO, hydrocarbons, halocarbons, alcohols, organic formates, benzene derivatives and such simple inorganics as nitrous oxide. Fields are created through dipole orientation, as numerous studies have now conclusively demonstrated. Spontlectric materials represent a new structural and electrical phase of solids. The spontlectric phase may be experimentally characterised by direct measurement of potentials on the surface of films of material\(^1\) or, as has been shown very recently, by reflection-absorption infrared spectroscopy (RAIRS).\(^8,9\)

This is the technique which is used in the present work.

The principle of the RAIRS experiment is as follows. The spontlectric field in the film creates a Stark shift\(^10\) in vibrational frequencies measured in RAIRS. Since the strength of the spontlectric field depends on the temperature of deposition of the film of material, there is a corresponding temperature dependence of the vibrational frequencies measured using RAIRS. For example the electric field in N\(_2\)O decreases by a factor of 2.3 between deposition temperatures of 48 K and 62 K.\(^1\) There is an accompanying Stark shift in vibrational energy levels, involved in the \(vNN\) stretch, of 1.2 cm\(^{-1}\). Such measurements of the shift in characteristic vibrational frequencies, as a function of deposition temperature, are diagnostic of the spontlectric effect. As discussed in detail in \[8\] and \[9\], volume changes of the material contribute negligibly to the temperature dependence of vibrational frequencies. Observed Stark shifts may then be used to characterise the spontlectric field in the material. The proof of principle of this method was provided by a RAIRS study of N\(_2\)O films\(^9\) and the technique has been used to study CO ices\(^6\), both deposited directly on a SiO\(_2\) surface. Here we extend these studies to include CO deposited on various forms of water ice, composed of crystalline solid water (CSW), compact amorphous solid water (cASW) and porous amorphous solid water (pASW).

The reasons for conducting the present study are twofold. First, we seek further to exploit the readily accessible technique of RAIRS as a means of performing new detections of the spontlectric effect in films, in this case of heterolayered films.\(^11\)

Second, and on a quite different tack, there are significant astrophysical applications, in the field of star formation, associated with solid CO on water ice. It is known through observation of these so-called pre-stellar cores, that CO is heavily depleted from the gas phase through condensation on interstellar grains\(^12,13\), already coated with a water ice mantle. The data which we present here show that such grains, with a CO layer on top of a water ice substrate, are likely to harbour several polarization charges. Following results in \[14\], we expect these polarization charges to be positive at the CO-vacuum interface. This could contribute to the low values of the observed degree of ionization in such prestellar cores.\(^15,16\)

The present report therefore supplies useful information for modelling of these noteworthy regions in the interstellar medium, which are on the verge of gravitational collapse to form a star.
As described in the experimental section 2, spontelectric films are studied using RAIRS with a grazing infrared beam. Thus the incident electric field of the beam has components both parallel and perpendicular to the film normal. Relative to the incident beam wavelength, the film can be considered infinite in the plane of the film and only transverse optical (TO) phonons can be excited in this plane. If however the thickness of the film is comparable to the wavelength of the incident beam, the boundary conditions allow for the excitation of longitudinal optical (LO) phonons along the normal axis. This is known as the Berreman effect\textsuperscript{17}, and has been studied extensively in non-ionic films.\textsuperscript{18,19,20}

Longitudinal phonons resonate at higher frequencies, because of the induced field associated with longitudinal waves passing through a medium composed of dipolar species. Thus when an incident beam interrogates a thin film at a suitably oblique angle, any vibrational mode has two components and is subject to so-called LO-TO splitting.

Henceforth \(v_L\) and \(v_T\) represent the frequencies for LO and TO phonons respectively and \(\Delta v = v_L - v_T\) represents the value of the splitting. The force fields giving rise to \(v_L\) and \(v_T\) are modified by the vibrational Stark effect, through the presence of the spontlectric field associated with the film of solid CO.

We have shown in detail in \[9\] how we may relate the resulting modification of LO-TO splitting, and its temperature dependence, to the presence of a static spontelectric field, oriented along the surface normal of the film. This is summarized in the present work in Section 3.

We then demonstrate how measurements of \(v_L\) and \(v_T\), as a function of deposition temperature, may then lead to a characterization of the spontlectric field in CO on CSW, \(c_{SW}\) and \(p_{SW}\). For simplicity, we refer throughout to the observed splitting in RAIR spectra as LO-TO splitting. At the same time, we recognize that the absolute value of the splitting arises through a combination of the intrinsically different vibrational frequencies associated with LO and TO modes and, at the level of approximation adopted here, an independent contribution due to the vibrational Stark effect. We find, for example, that at a deposition temperature of 20 K, the Stark effect contributes 54\% of the total measured splitting of 4.59 cm\(^{-1}\) for CO deposited on CSW (CO-CSW).

Moreover, the observed deposition temperature dependence of LO-TO splitting, in this case of 4.59 to 4.18 cm\(^{-1}\) between temperatures of 20 K and 24 K, may be attributed wholly to the dependence of the spontlectric field on the film deposition temperature.

2. Experimental method and results

2.1. The experimental method

RAIRS experiments were performed using an ultrahigh vacuum system, described in detail elsewhere.\textsuperscript{21,22} The substrate, an oxygen-free high conductivity copper block coated with 300 nm of amorphous silica, is mounted on the end of a closed-cycle helium cryostat, reaching a base temperature of 18 K, measured with a KP-type thermocouple connected to an II-6 temperature controller (II Instruments). The central chamber is equipped with a line-of-sight quadrupole mass spectrometer (QMS, Hiden Analytical) and a Fourier-transform infrared spectrometer (Varian 670-IR) used in reflection-absorption mode, at a grazing incidence of 75\° with respect to the normal to the substrate. After reflection from the sample, the infrared beam is focused into a liquid nitrogen cooled HgCdTe detector. The RAIR spectra presented here result from co-addition of 512 spectra recorded at a resolution of 0.1 cm\(^{-1}\).

The layered films, consisting of 20 ML of CO on 50 ML of water, are deposited by background dosing of H\(_2\)O (Fluka, purity 99.9 \%) and CO gas (BOC, purity 99.9\%) onto the substrate at a rate of 0.04 ML s\(^{-1}\) and 0.05 ML s\(^{-1}\), respectively. Deposition of H\(_2\)O at a substrate temperature of 18 K, 110 K and 140 K ensured respectively, \(p_{ASW}\), \(c_{ASW}\) and CSW.\textsuperscript{23,24,25,26} The substrate was cooled and CO was dosed at 20 K, 22 K or 24 K, save for CO-\(c_{ASW}\) in which the lowest temperature of dosing was 21 K. Thicknesses of H\(_2\)O and CO films in monolayers (ML) were determined (±20\%) through temperature-programmed desorption (TPD) experiments, performed by applying a heating ramp of 0.2 K s\(^{-1}\) for CO desorption and 0.1 K s\(^{-1}\) for H\(_2\)O desorption from the base temperature of 18 or 20 K. The desorbed species were detected using the QMS.

2.2. Results

The RAIR spectra of the vCO band of 20 ML CO deposited as CO-CSW, CO-\(p_{ASW}\) and CO-\(c_{ASW}\) at various temperatures are presented in Figure 1, a, b and c, respectively. The inserts in Figure 1 show the change in the appearance of the OH stretching band of H\(_2\)O in CSW, \(p_{ASW}\) and \(c_{ASW}\).
Figure 1: RAIR spectra collected after CO has been deposited at 20 or 21 (black), 22 (red) and 24 (blue) K on CSW (a), pASW (b) and cASW (c). The inserts in each graph show the OH stretch for the water substrate beneath the CO layer. In each case a contraction in the LO4 TO splitting of the CO stretching mode is seen as the deposition temperature increases.

The CO band exhibits LO-TO splitting, with the LO mode for example at 2142.96 cm$^{-1}$ and the TO mode at 2138.08 cm$^{-1}$ at 20 K for CO-pASW. The LO mode red-shifts while the TO mode blue-shifts as the deposition temperature is increased from 20 K to 24 K, as Figure 1 shows. Data for RAIRS spectra of CO at deposition temperatures above 24 K are not presented, since desorption from the different water substrates occurs at these higher temperatures, unlike CO deposited directly on the SiO$_2$ surface$^{3,28}$. Just as for CO films deposited directly on SiO$_2$ and annealed, annealing CO films deposited on the H$_2$O layers does not produce detectable shifts in the LO and TO modes. Desorption of CO was not observed at the temperatures used for this work as confirmed by TPD experiments$^{27}$ and a vCO band intensity was found to be constant within ~6% during the annealing experiment from a base temperature of 20 K to 24 K.

The LO and TO modes of the vCO band of CO films on the different H$_2$O substrates were fitted with Gaussian functions using the Igor Pro software, following a procedure described in [9]. This gave an accuracy of ±0.01 cm$^{-1}$ and ±0.02 cm$^{-1}$ for the location of the peak maximum of the LO and TO modes, respectively. Figure 2 has been constructed from this analysis showing the peak positions of the LO and TO modes of CO-pASW (blue), CO-cASW (red) and CO-CSW (black) with respect to deposition temperature. The red-shift of the LO band and the blue shift of the TO band, with increasing deposition temperatures, may clearly be seen in Figure 2.

The continuum between the LO and TO peaks is created through inhomogeneous broadening. Greater broadening indicates a larger range of molecular environments and here we briefly consider the connection with the degree of dipole orientation with reference to the underlying ice structure. Measurement of the broadening was performed from the intensity of the RAIR spectra at 2141 cm$^{-1}$, essentially the average of the LO and TO modes, and normalising this with the integrated area of the entire vCO band. This normalisation allows the inhomogeneous broadening to be compared between different experiments at different temperatures, on any one material. Figure 3 shows this measurement for the CO film on the various H$_2$O underlayers. Insofar as inhomogeneous broadening, for any one of the three cases, is a measure of the range of environments in which any CO species finds itself, the greater the inhomogeneous broadening the less the dipole orientation. Results in Figure 3 are therefore consistent with the expected behaviour of a spontaneous material, and may be understood to show the expected drop in dipole orientation with increasing deposition temperature.$^1$
terms obtained directly from experimental data

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tr>
<td>$\nu_L$</td>
<td>longitudinal optical (LO) frequency</td>
</tr>
<tr>
<td>$\nu_T$</td>
<td>transverse optical (TO) frequency</td>
</tr>
<tr>
<td>$\Delta \nu$</td>
<td>measured LO–TO splitting</td>
</tr>
<tr>
<td>$\Delta \nu_S$</td>
<td>splitting due to the spontelectric Stark field</td>
</tr>
<tr>
<td>$\Delta \nu_B$</td>
<td>intrinsic splitting</td>
</tr>
<tr>
<td>$\xi$</td>
<td>$\Delta \nu_S/\Delta \nu$</td>
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</table>

terms involved in modelling

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tr>
<td>$\mu$</td>
<td>dipole moment of CO in the solid state</td>
</tr>
<tr>
<td>$&lt;\mu&gt;/\mu$</td>
<td>degree of dipole orientation</td>
</tr>
<tr>
<td>$\Omega$</td>
<td>parameter related to the molecular volume of CO</td>
</tr>
<tr>
<td>$T$</td>
<td>temperature of deposition</td>
</tr>
<tr>
<td>$\xi$</td>
<td>locking term parameter in Equation (2)</td>
</tr>
</tbody>
</table>

Table 1: Glossary of symbols used in Section 3.

3.1 Data in tabular form

The data shown in Figures 1a, b and c are shown in tabular form in Tables 2, 3 and 4 for CO-CSW, CO-pASW and CO-cASW respectively.

Table 2: RAIRS data for CO-CSW. Column 1: deposition temperature. Columns 2,3: the frequency of the TO, LO vibrations. Column 4: the total LO–TO splitting. Column 5: the contribution of the spontelectric Stark effect to the total LO–TO splitting, based upon $\Delta \nu_B = 2.119 \text{ cm}^{-1}$ (see text). Column 6: the ratio of the Stark effect splitting to the total.

<table>
<thead>
<tr>
<th>T / K</th>
<th>$\nu_{\text{TO}}$/ cm$^{-1}$</th>
<th>$\nu_{\text{LO}}$/ cm$^{-1}$</th>
<th>$\Delta \nu$/ cm$^{-1}$</th>
<th>$\Delta \nu_S$/ cm$^{-1}$</th>
<th>$\xi = \Delta \nu_S/\Delta \nu$</th>
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<td>2142.47</td>
<td>4.18</td>
<td>2.061</td>
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</table>

Table 3: RAIRS data for CO-pASW. Column 1: deposition temperature. Columns 2,3: the frequency of the TO, LO vibrations. Column 4: the total LO–TO splitting. Column 5: the contribution of the spontelectric Stark effect to the total LO–TO splitting, based upon $\Delta \nu_B = 2.119 \text{ cm}^{-1}$ (see text). Column 6: the ratio of the Stark effect splitting to the total.

<table>
<thead>
<tr>
<th>T / K</th>
<th>$\nu_{\text{TO}}$/ cm$^{-1}$</th>
<th>$\nu_{\text{LO}}$/ cm$^{-1}$</th>
<th>$\Delta \nu$/ cm$^{-1}$</th>
<th>$\Delta \nu_S$/ cm$^{-1}$</th>
<th>$\xi = \Delta \nu_S/\Delta \nu$</th>
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<td>21</td>
<td>2138.08</td>
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<td>4.88</td>
<td>2.761</td>
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<tr>
<td>22</td>
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<td>2142.82</td>
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<tr>
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<td>2138.34</td>
<td>2142.43</td>
<td>4.09</td>
<td>1.971</td>
<td>0.482</td>
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Table 4: RAIRS data for CO-cASW. Column 1: deposition temperature. Columns 2,3: the frequency of the TO, LO vibrations. Column 4: the total LO–TO splitting. Column 5: the contribution of the spontelectric Stark effect to the total LO–TO splitting, based upon $\Delta \nu_B = 2.119 \text{ cm}^{-1}$ (see text). Column 6: the ratio of the Stark effect splitting to the total.

<table>
<thead>
<tr>
<th>T / K</th>
<th>$\nu_{\text{TO}}$/ cm$^{-1}$</th>
<th>$\nu_{\text{LO}}$/ cm$^{-1}$</th>
<th>$\Delta \nu$/ cm$^{-1}$</th>
<th>$\Delta \nu_S$/ cm$^{-1}$</th>
<th>$\xi = \Delta \nu_S/\Delta \nu$</th>
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<tr>
<td>21</td>
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<td>2142.89</td>
<td>4.81</td>
<td>2.891</td>
<td>0.559</td>
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<tr>
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<td>2142.89</td>
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<td>0.558</td>
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<tr>
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<td>2142.63</td>
<td>4.34</td>
<td>2.221</td>
<td>0.512</td>
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The total splitting observed, $\Delta \nu$, is a sum of that part due to the spontelectric field, $\Delta \nu_S$, plus the intrinsic LO–TO splitting, $\Delta \nu_B$. If we plot the observed LO–TO splitting versus $T^3$ and extrapolate to high $T$, as in [9], we find for example for the CO-CSW data that $\Delta \nu_B = 2.119 \text{ cm}^{-1}$. This may be compared with the value of $\Delta \nu_B = 2.59 \text{ cm}^{-1}$ for CO-SiO$_2$. 

Figure 3: Intensity measured at 2141 cm$^{-1}$ in the RAIR spectra normalized by the total area of the $\nu$CO band for each substrate, as a function of deposition temperature. The dotted line results from a linear fit of the data and is only presented here to guide the eye.
Numerical experiments show however that parameters derived for the spontelectric field are robust to a range of values of $\Delta V_b$. For example for CO deposited at 22 K on CSW ice, the spontelectric field is found to be $2.84 \times 10^7$ \text{V/m}$ using $\Delta V_b = 2.59$ \text{cm}^{-1}$ and $2.79 \times 10^7$ \text{V/m}$ using $\Delta V_b = 2.119$ \text{cm}^{-1}$, a variation in the field of $<2\%$. This may be compared with an error resulting from random experimental uncertainties of $\pm 5\%$.

The grounds for this lack of sensitivity, of the derived field to the absolute values of splitting, is that the derived spontelectric field is most influenced by the temperature dependence of $\Delta V_b$, rather than the absolute values. This is clear from the analysis presented in [8] in sections 3.4.2, 3.4.3 and results shown in Table 2 of that paper. Moreover the intuitive notion that a greater spontelectric Stark field should lead to a \textit{proportionally} larger spontelectric splitting does not hold, as we see below. In Tables 2, 3 and 4, we have used $\Delta V_b = 2.119$ \text{cm}^{-1}. We also present our conclusions, in section 3.3, for both $\Delta V_b = 2.119$ \text{cm}^{-1} and $2.59$ \text{cm}^{-1}, to emphasise the insensitivity of the derived spontelectric field to our lack of accurate knowledge of $\Delta V_b$. Thus uncertainties in the derived spontelectric fields and the degrees of dipole orientation include the effect of possible systematic errors in $\Delta V_b$.

3.2. The model for the spontelectric effect
A detailed description of a model for the spontelectric effect may be found in [1]. This introduces the concept that constituent molecules in the film experience (i) a local symmetric field, $<E_{sym}>((1+\xi(<\mu_z>/\mu)^2)$, where $<E_{sym}>$ and $\xi$ are derived from fitting to experimental data. Here $<\mu_z>/\mu$, is the temperature dependent degree of dipole orientation, defined as the ratio of the average $z$-component of the dipole moment and the total dipole moment of the molecular species in the solid state. (ii) An asymmetrical field, the spontelectric field, $E_{sp}$, given by $4\pi(<\mu_z>/\mu)$ $\mu$/$\Omega$, where $\Omega$, related to the molecular volume, may be treated as a parameter of the model.

The net field in the $z$-direction, normal to the plane of the film, is given by

$$E_z = \left[\frac{1+\xi(<\mu_z>/\mu)^2}{\mu}\right]E_0$$

We note that the symmetrical part of the contribution to $E_z$ is related to the ‘local field’ at any molecular site, as defined in standard texts.\textsuperscript{30}

Mean field theory gives an implicit expression for $<\mu_z>/\mu$, yielding the familiar Langevin function for orientational interactions\textsuperscript{30}

$$\frac{<\mu_z>}{\mu} = \coth\left(\frac{E_0<\mu_z>/\mu}{T}\right) - \left(\frac{E_0<\mu_z>/\mu}{T}\right)^{-1}$$

where $T$ is the deposition temperature of the layer of material. Note that atomic units (au) are used here, in which the Boltzmann constant is unity and $e_0$ is $1/4\pi$.

Dipole moments in the solid state are reduced from those in the gas phase through depolarization according to:

$$\mu = \frac{\mu_0}{1 + \varepsilon k s^2}$$

where $s$ is the average spacing between successive layers, $\alpha$ is the molecular polarizability for CO (13.159 au), $k = 11.034^{11}$ and $\mu_0$ is the gas phase dipole moment, which for CO is 0.122 D. $s$ is estimated for CO from the diameter of isoelectronic N\textsubscript{2} to be 0.339 nm or 6.406 au. In the absence of any other data, $s$ is assumed to take on the same value for CO-\textsubscript{pASW}, CO-\textsubscript{cASW} and CO-CSW.

3.3 Derivation of spontelectric fields in CO-CSW, CO-\textsubscript{pASW} and CO-\textsubscript{cASW}.
It was shown in [8] and [9] that (U\textsubscript{1} - U\textsubscript{3} - U\textsubscript{T}) $\Delta V$ $\nu_T$, where U\textsubscript{T} is the energy associated with the TO vibration and U\textsubscript{3} with the LO vibration. Additionally, U\textsubscript{1} - U\textsubscript{T} $\propto$ the spontelectric field times the degree of dipole orientation and U\textsubscript{T} $\propto$ to the symmetric part of the field times $\Delta V$/$\Omega$. That is, $U_T = \xi^4 <E_{sym}> (1 + \xi(<\mu_z>/\mu)^2)$, where $\xi = \Delta V_b/\Delta V$. Including an additional independent term describing the intrinsic LO-TO splitting, $\Delta V_b$, we obtain

$$\frac{\Delta V}{\nu_T} = \frac{\xi^4 E_0}{\{1 + \xi(<\mu_z>/\mu)^2\}} \frac{\Delta V_b}{\nu_T}$$

Combining Eq. 1 and 2 and using coth (x) $\sim$ 1/x $\sim$ 1/3 x, it may be shown that

$$\frac{<\mu_z>/\mu}{\mu} = \frac{3T - \sqrt{2\mu^2 \xi^4 \{E_0 \{E_0 - \{E_0\}}\}} + 9T^4}{2\mu^2 \xi^4 \{E_0 \}}$$

From which it follows, using Eq. 4 and $\Delta V = \Delta V_b + \Delta V_b$, that

$$\Delta V_b = \frac{\mu^2 \xi^4 E_0 T}{E_0 \{3T - \sqrt{2\mu^2 \xi^4 \{E_0 \}} + 9T^4\}} - \frac{6\xi^4 \{E_0\}}{V_T}$$

Since E\textsubscript{0} = $4\pi(<\mu_z>/\mu)$ $\mu/\Omega$, we can therefore derive $(<\mu_z>/\mu)$ from

$$<\mu_z>/\mu = \Omega E_0 / 4\pi \mu$$

We now set $\xi = 43.8$, the value associated with N\textsubscript{2}O, choosing this value since both the layer spacing and the
dipole moment of N₂O and CO in the solid state are closely similar. In this connection, Δvₜₜ, evaluated through equation (6), is insensitive at the <5% level to any relevant range of values of ζ, between tens to >10⁶.

We now proceed as in [9], summarised as follows. With the help of Eqns. 4 to 7, we estimate <E_{sym}> from three pairs of simultaneous equations, each pair for two temperatures, use the resulting value of <E_{sym}> to obtain a value of Ω for a specific temperature, and use this to obtain Eₜₜ and an estimate of <μₜₜ>/μ. This sequence is performed for each of CSW, p-ASW and c-ASW for both Δv₁ = 2.119 cm⁻¹ and 2.59 cm⁻¹. Results are shown in Table 5. Values of Eₜₜ and <μₜₜ>/μ may be seen to be insensitive to the choice of Δv₁, as noted earlier.

<table>
<thead>
<tr>
<th></th>
<th>&lt;E_{sym}&gt;/10⁶ V m⁻¹</th>
<th>Eₜₜ/10⁶ V m⁻¹</th>
<th>&lt;μₜₜ&gt;/μ</th>
<th>Δv₁/cm⁻¹</th>
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<tbody>
<tr>
<td></td>
<td>± 0.1 × 10⁷</td>
<td>± 0.15 × 10⁷</td>
<td>± 0.0024</td>
<td></td>
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</tr>
<tr>
<td></td>
<td>1.96</td>
<td>1.80</td>
<td>1.86</td>
<td>0.0097</td>
</tr>
<tr>
<td>SiO₂</td>
<td>4.48</td>
<td>3.78</td>
<td>3.72</td>
<td>3.66</td>
</tr>
</tbody>
</table>

Table 5: Values of <E_{sym}>, of the spontelectric field, Eₜₜ, and of the degree of dipole orientation for CO deposited on the three underlying substrates, crystalline solid water (CSW), porous amorphous solid water (p-ASW) and compact amorphous solid water (c-ASW) for deposition temperatures of 20, 22 and 24 K. Values shown are the upper branch solutions, as discussed in 3.3. Data are also shown for CO deposited on SiO₂, taken from [9]. Uncertainties given are random errors. Values are also quoted for both an intrinsic splitting, Δv₁ₜₜ, of 2.119 cm⁻¹ and of 2.59 cm⁻¹ (see text). * for data taken at 21 K deposition temperature.

As in [9], the procedure outlined above did not yield a unique value of Ω. For each case of CO-p-ASW, CO-c-ASW and CO-CSW, two groups of values were encountered. One group consisted of low average values of 20, 14 and 39 au⁴ for CO-CSW, CO-p-ASW and CO-c-ASW respectively and another group of high values, 172, 235 and 83 au⁴. A recent paper¹² reported the correlation between polarizability, α, and molecular volume and suggested the empirical relationship α = 0.0086 Ω⁴⁵. Using α = 13.159 au, we find Ω₈₉ₐ = 244±30 au. Evidently this would favour the group of higher values of Ω, which we have used in preparing Table 5. For comparison, the value of Ω for CO-SiO₂ was found to be 273 au in [9].

Solutions of Equation (6) for the spontelectric field yield two values for each deposition temperature and each ice substrate, with corresponding values of the degree of dipole orientation. For example CO-p-ASW at 20K has a field of both 3.73 × 10⁷ V m⁻¹ and 8.79 × 10⁶ V m⁻¹, referred to as the upper and lower branches respectively, representing a bi-metastable system as discussed briefly in [9]. In order to attempt to choose between these two sets values, we have recourse to values of the vibrational Stark shift of CO in the gas phase. Following these values, average fields presented in Table 5, that is, for the upper branch, would create a typical Stark shift of 0.71, 0.91 and 0.49 cm⁻¹ respectively for CO-CSW, CO-p-ASW and CO-c-ASW. Values associated with the lower branch of the spontelectric field would be 0.17, 0.2 and 0.12 cm⁻¹. Observed Stark shifts are 0.89, 0.98 and 1.02 cm⁻¹ respectively, using the average values of Δv₂/2 with Δv₁ = 2.59 cm⁻¹. Thus values for CO-CSW and CO-p-ASW favour the adoption of the upper branch values of the spontelectric field, while values for CO-c-ASW may leave some doubt. We will use values of the upper branch for all three cases in the remainder of this paper.

4. Discussion of results

4.1 Comparison with CO films on SiO₂

Results in Table 5 show three distinct regimes within the uncertainties associated with the data. First, CO deposited on p-ASW has an essentially indistinguishable spontelectric field from CO-SiO₂. The corresponding degree of dipole orientation at 20K is 0.0506±0.004, taking the average of values in Table 5. This figure is ~20% lower than for CO-SiO₂. Equation (7) implies a correspondingly smaller value of Ω, and we find a value ~15% lower. Second, CO-c-ASW, by contrast with CO-p-ASW, shows a markedly weaker field than CO-SiO₂ films. Third, the spontelectric field for CO-CSW lies between CO-p-ASW and CO-c-ASW. In addition, experimental errors in values of the spontelectric field obscure the detection of any trend of increase in the field with decreasing temperature of deposition.

The difference in the behaviour of CO-c-ASW, CO-CSW and CO-p-ASW may most simply be attributed to a different structure of the CO film in each case. The only parameter in the model which can be directly related to the aspect of
structure, is the value of the effective molecular volume. Values lie in the approximate ratio 1 : 2 : 2.8 for CO-$c_{\text{ASW}}$, CO-CSW and CO-$p_{\text{ASW}}$. This may be related to different porosities in each case, where the underlying water structure templates the CO. This suggestion is supported by data for inhomogeneous broadening shown in Figure 3, section 2.2. Another speculative explanation may lie in the postulate that differing dipoles, created at the ice-CO interface, may influence the magnitude of an effective field in the overlying layer of CO.\textsuperscript{11} In this case, the measured Stark effects would arise from a superposition of the spontelectric field and a spatially decaying field which arises from the interfacial dipole. The latter field would most likely be different for each type of underlying ice layer. Note that the presence of such a decaying non-spontelectric field is omitted from our analysis.

4.2 Relevance of spontelectric grains to astrophysical processes in regions of future star and planet formation: prestellar cores

There exist many examples in the Milky Way of dense condensations of gas, so-called prestellar cores, of dimension of a few tenths of a parsec (1pc $\sim$3 $\times$ 10$^6$ m), where ‘dense’ implies local pressures of around 10$^{13}$ mbar. A number of observations show that the degree of ionization in these cores may be a factor of five to ten lower than elsewhere in the UV-shielded part of the interstellar medium (ISM)\textsuperscript{43,44}; given that the standard cosmic ray induced ionization fraction should be $\sim$3 x 10$^{-8}$ for a core of density $\sim$10$^5$ cm$^{-3}$,\textsuperscript{34,35,36} This has important consequences for the early stages of star formation, for example (i) via the chemistry and associated cooling rate, where heat is generated through gravitational contraction and requires to be lost to allow gravitational collapse, and (ii) through the weakness of measured magnetic fields encountered in these regions (see section 4.2.3). We show below that the presence of polarization charging on the surface of grains, as our experimental data suggest, may lead to an understanding of the low level of ionization, from which springs so many properties related to star formation.

It is well-known from observation that CO is strongly depleted from the gas phase by freezing out onto interstellar grains in prestellar cores, as described for example in [37]. The layer of CO so formed would be almost pure or diluted somewhat in N$_2$, to an unknown extent. We choose here to ignore this possible dilution, noting that dilution of the spontelectric material N$_2$O in Xe, in equal quantities, reduces the spontelectric field by only $\sim$35\%\textsuperscript{7}. We recognize also that some CO may be converted to CO$_2$\textsuperscript{38}. According to the experimental results presented here, grains in sufficiently cold regions, at $\lesssim$26K, will therefore possess a polarization surface charge through the spontelectric effect. The remit in this section is limited to setting out some of the microscopic physics which arises from the possible presence of spontelectric CO ices on grains. In section 4.2.1, we consider the rate of accumulation of CO ice mantles on grains and show that essentially all CO in the gas phase should be absorbed onto dust grains, as indeed can be observed. In section 4.2.2 we estimate the rates of electrons and ions colliding with grains, using theory set out in [39] as a guide. In section 4.2.3 we outline the effect that spontelectric grains will have on the degree of ionization of the interstellar gas.

Pre-stellar cores are masses of weakly ionized plasma on the verge of gravitational collapse to form protostars. We use typical physical conditions which may be obtained, directly or indirectly, from observations of these cores. Such objects are found in a variety of environments, some of which they may be rather isolated from any obvious external activity, such as the Bok globule B68 (e.g. [40] and references therein), or others which may be closely associated with shocks from recently formed massive stars, such as in Orion.\textsuperscript{41} Since B68 is the most intensively studied, we use physical conditions found there as a guide. These are as follows: number density of H$_2$, $n_{\text{H}_2}$ = 10$^5$ cm$^{-3}$, [CO]/H$_2$ = 10$^{-4}$ and kinetic temperature, $T$ = 10 K. We note that pre-stellar cores can possess a range of conditions; see section 4.2.3. Observational data\textsuperscript{40,42,43}, with data for the grain density, taken here to be 2 g cm$^{-3}$, and the proportion of the mass of the ambient medium contained in grains (0.013)\textsuperscript{44}, may be used to evaluate how many ML of CO may be found on a ‘typical grain’. This may be shown to be $\sim$12 ($a_a$/0.1)$^{3/2}$ ML taking account of a small increase of grain radius as adsorption progresses (see section 4.2.1). Here $a_a$ = grain radius in $\mu$m where this value is generally taken to be 0.1 $\mu$m\textsuperscript{45}. Following recent data in [46], the thickness of H$_2$O ice on grains should be limited to $\sim$30 ML as a maximum, increasing the effective grain radius by $\sim$10\%, which we choose to ignore at this stage. The regions considered are sufficiently dense that UV radiation is excluded from the gas and grain charging is controlled by collisions with electrons and ions.

Water ice spectra, from observations of the ISM, show that generally the ice is in the form of compact amorphous ice\textsuperscript{47}, referred to as $c_{\text{ASW}}$ above. In the subsequent analysis we therefore assume that the number of volts added per ML of CO, $\phi$ = 6.695 x 10$^3$ V ML$^{-1}$, using the value for 21 K. In this connection, it is possible that the $p_{\text{ASW}}$ substrate in our experiments itself harboured a surface potential.\textsuperscript{48} All symbols used in the forthcoming sections are defined in Table 6.
Inserting values of $T = 10$ K, appropriate for B68, $a_b = 10^{-7}$ m and $s = 0.339$ nm, we find the variation of $[\text{CO}]$ with time shown in Figure 4. In this figure it may be seen that effectively complete depletion (99.8% complete) takes place in $9 \times 10^{12}$ seconds $= 2.85 \times 10^9$ years.

**Figure 4**: the removal of CO with respect to time from the gas phase, initially at $10^7$ m$^{-3}$, through condensation onto dust grains, according to Eq.9. The physical conditions are CO/H$_2 = 10^5$, $n_{\text{CO}} = 10^{11}$ m$^{-3}$, $T = 10$ K, initial grain radius at $t = 0$, $a_b = 10^{-7}$ m, with other relevant parameters given in Table 6.

The time to form one ML is inversely proportional to CO, itself decreasing rapidly with time, and increases from an initial value of $1.8 \times 10^3$ seconds ($\sim$5700 years) to form 1 ML, rising to $1.2 \times 10^5$ seconds ($3.7 \times 10^4$ years) to form 5 ML and $4.0 \times 10^5$ seconds ($1.3 \times 10^5$ years) to form 10 ML. The corresponding growth of the CO film in terms of $n_{\text{ML}}$ versus time is shown in Figure 5, where it may be seen that the film achieves $\sim$12 ML. The growth of the film will be accompanied by a growth in the positive polarization charge on the grain surface. This will be attended by an enhanced collision rate of electrons with the grain. We now address the question, in 4.2.2 below, of the relative timescales for CO condensation on the grain and the rate of electron collisions which tend to remove the spontelectric potential from the surface of the grain.

**4.2.1 Accretion of CO ice mantles**

As mentioned above, CO is strongly depleted in the denser part of pre-stellar cores, for example in B68$^{29}$ or in L1689B$^{30}$. Therefore it might be sufficient simply to state that for $a_b = 0.1$ µm, dust grains are covered by 10 to 15 ML (see above) and leave it at that. However it is our purpose here to compare timescales of CO accretion and ion and electron collisions with the grain in order to gain physical insight into the nature of spontelectric grain charging. We therefore seek first to show that almost all the available gas phase CO can condense on grains well within the lifetime of a pre-stellar core, which has been variously estimated but may be typically $\sim$4.5 $\times$ 10$^5$ years.$^{50,51}$ The time of depletion has been estimated in earlier work (e.g. [52]) but the analysis was incomplete since the process was treated as exponential in time, treating the grain radius as independent of the quantity of CO adsorbed.

The first order rate coefficient, $k^{114}$, for removal of gas phase CO onto the grain surface is given by the velocity of CO times the cross-section presented by the grain. The number of grains per m$^3$ is given by $2.1 \times n_{\text{H}_2}m_{\text{H}_2}/\pi a_b^2$, with each presenting a cross-section for CO of $a^2$, where $a$ is the radius of the grain at time $t$. As time progresses, the radius of the grain will increase by $n_{\text{ML}}s$, where $n_{\text{ML}}$ is the number of monolayers and $s$ is the layer spacing (see Table 6). Hence

$$k^{114} = (2.1 \times n_{\text{H}_2}m_{\text{H}_2}/\pi a_b^2) \times a^2 \times (8kT/\pi m_{\text{CO}})^{1/2} = 6.26 \times 10^{-31} n_{\text{H}_2} T^{1/2} a$$  \hspace{1cm} (8)

where $a$ is a function of time. The rate of change of radius with time is given by $da/dt = s = d[n_{\text{H}_2}]/dt = 6.849 \times 10^{-6}$ s [CO] given that 1 ML requires $10^{19}$ CO molecules m$^{-2}$. Therefore that the time to form a ML is $4 \times 10^5/(8kT/\pi m_{\text{CO}})^{1/2}$[CO]](CO). This yields $n_{\text{ML}} = 6.849 \times 10^{19}$[CO]t. Thus the radius $a_b$ as a function time follows $a = 6.849 \times 10^{19}[\text{CO}] t + a_b$ where $a_b$ is the bare, or water ice covered, grain radius $= 10^{-7}$ m.

Thus we obtain:

$$d[\text{CO}]/dt = -[\text{CO}] [(6.26 \times 10^{-31} n_{\text{H}_2} T^{1/2})/a_b + 6.849 \times 10^{-19}[\text{CO}] t s]$$  \hspace{1cm} (9)

**Table 6**: Symbols used in section 4. Standard values are shown in brackets.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$n_b$</td>
<td>Number of grains per unit volume</td>
</tr>
<tr>
<td>$m_{\text{H}_2}$</td>
<td>Mass of H atom, CO molecule</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>Degree of ionization of the medium relative to $n_{\text{H}_2} (5 \times 10^4)$</td>
</tr>
<tr>
<td>$n_{\text{H}_2}$</td>
<td>Number of H$_2$ molecules per unit volume ($10^{11}$ m$^{-3}$)</td>
</tr>
<tr>
<td>$T$</td>
<td>Kinetic temperature (10 K)</td>
</tr>
<tr>
<td>$T_e$</td>
<td>Electron temperature (10 K)</td>
</tr>
<tr>
<td>$s$</td>
<td>Layer spacing (0.339 nm)</td>
</tr>
</tbody>
</table>
permanently attached to polycyclic aromatic hydrocarbons positively charged. These expressions involve essentially a by the charge of the incident particle, here an electron or an neutralization by gas phase electrons of the positive It is our purpose here to consider timescales for electron grains. In a seminal paper of 1987, entitled ‘Collisional Charging of interstellar Grains’\textsuperscript{39}. Draine and Sutin derived expressions for the rate of collisions of electrons with grains, for grains which are negatively charged, neutral and positively charged. These expressions involve essentially a cross-section times a velocity, in the normal manner, but multiplied by a factor, \( f(\nu; \tau) \) which takes account of enhancement or reduction due to the charge state of the grain. \( \nu \) is a signed quantity equal to the charge on the grain divided by the charge of the incident particle, here an electron or an ion, and \( \tau \) is a reduced temperature defined in \textsuperscript{39}. Account is taken, in estimating \( f(\nu; \tau) \), of the electrostatic polarization of the grain by the approaching electron and the associated image potential. We treat the electrons as free particles and in this work ignore the possibility that any significant fraction is permanently attached to polycyclic aromatic hydrocarbons (PAHs).\textsuperscript{53}

The conventional part of the rate coefficient in \textsuperscript{39} is given by the electron velocity in the plasma multiplied by the cross-sectional area of the grain. The first issue is therefore to determine the electron velocity. Electrons are formed at typically 20 eV by cosmic ray ionization of \( \text{H}_2 \) in shielded regions, as here. Electron energy is reduced rapidly to \(-10\) eV through electronically inelastic collisions and, below this energy, electrons are cooled very largely by elastic collisions with \( \text{H}_2 \), with a cross-section\textsuperscript{54,55} typically of \(-7.5\) Å\(^2\), which is approximately collision energy independent. Using our standard figure of \( n_{\text{H}_2} = 10^{11} \) m\(^{-3}\) and that each elastic collision removes \(-0.05\) meV from the electron energy, \(-9 \times 10^6\) seconds is required for removal of 10 eV and to equilibrate with the kinetic temperature. We therefore set the effective electron temperature at the ambient kinetic temperature, since that this cooling is fast compared with other relevant processes, such as the accumulation of CO layers. We also note that the interstellar medium with \( n_e = 500 \) m\(^{-3}\) (\( \alpha = 5 \times 10^{-7} \) \text{ cm}^{-3} \) \text{ s} \(-1\)) and \( T_e = 10\) K, our standard conditions, has an associated Debye length of \(-10\) m. Grains have a density of 0.73 m\(^3\) (see below) near the centre of B68, and thus the average distance apart of two such grains is \(-1.4\) m. Notwithstanding, we will assume that the plasma remains quasi-neutral. Further, a simple estimate shows that electric fields due to electron and positive ion differential drift are negligible and therefore electrons and ions may be assumed to perform independent ballistic trajectories. Note also that, throughout, the influence of magnetic fields is ignored.

According to \textsuperscript{39}, the rate of electron or ion collisions per second with grains is given by

\[
J_e = n_e s_e (kT_e/\mu_e)^{1/2} \pi \alpha^2 f(\nu; \tau)
\]

or

\[
J_i = n_i s_i (kT_i/\mu_i)^{1/2} \pi \alpha^2 f(\nu; \tau)
\]

where \( f(\nu; \tau) = [1 + (\pi^2 \nu^2)^{1/2}] \exp(-\nu^2/\tau) \) (attractive), \( 1 + (\pi^2 \nu^2)^{1/2} \) (attractive), \( \nu \tau = 1 + (\pi^2 \nu^2)^{1/2} \) (repulsive) for negatively charged, neutral and positively charged grains and where \( \theta_e = \nu/(1+\nu^2/\tau) \). Here, \( \nu \) is a positive or negative number, as appropriate, whose absolute value equals that of the effective charge on the grain, \( s_e \) and \( s_i \) are the sticking coefficient for electrons and ions on grains.

For our case of a neutral plasma, with \( n_e = 0.1 \) \( \mu \) m and \( n_{\text{H}_2} = 10^5 \) cm\(^{-3}\), we take the prevalent ion\textsuperscript{44} to be \( \text{H}^+ \), that is, reduced mass \( \mu_{\text{H}^+} = 1 \), noting that this might require modification according to models presented in \textsuperscript{56}. From this choice of the prevalent ion, it follows that \( s_{\text{H}^+}^2 = s_{\text{e}}^2 = \mu_{\text{H}^+} = 1 \), that is, 100% sticking efficiency may be assumed for both ions and electrons.\textsuperscript{57,58} The principle to which we adhere is that the flux of electrons and positive ions to the grain must be equal on a time average and we find that we should set \( \tau = 0.1 \) to 0.2 in order that this may approximately hold. This implies a charge on the grain of \( 1/[1 + (\tau \nu)^{1/2}] \approx -0.91 \) where \( s_e = 1.39 \times 10^{-3} \). Thus the average grain charge is negative, to repel the faster electrons and to attract the slower ions, as for any insulator immersed in neutral plasma. Throughout, we ignore any possible contribution from metal ions\textsuperscript{59}, such as Na\textsuperscript{+}.

Using equation (10), the timescales of encounters of relevance may be estimated. These estimates will be used in 4.2.3 for an assessment of the effect of spontelectric grains in the medium. Table 7 shows timescales for encounters of interest. The values of grain charge represent an initial value estimated above of -0.91, neutral grains and the value
obtained by removal of an electron, that is, +1.09. An important conclusion is that all characteristic times are very short compared with the time to form 1 ML, say, of CO, which we estimated in 4.2.1 was typically $>2 \times 10^7$ seconds.

<table>
<thead>
<tr>
<th>Projectile</th>
<th>Grain charge</th>
<th>Lifetime to encounter / s</th>
</tr>
</thead>
<tbody>
<tr>
<td>e</td>
<td>-0.91</td>
<td>1 to $2 \times 10^7$</td>
</tr>
<tr>
<td>e</td>
<td>Neutral</td>
<td>$10^9$</td>
</tr>
<tr>
<td>e</td>
<td>1.09</td>
<td>$3 \times 10^5$</td>
</tr>
<tr>
<td>H(^+)</td>
<td>-0.91</td>
<td>1 to $2 \times 10^7$</td>
</tr>
<tr>
<td>H(^+)</td>
<td>Neutral</td>
<td>$4 \times 10^7$</td>
</tr>
<tr>
<td>H(^+)</td>
<td>1.09</td>
<td>1 to $2 \times 10^9$</td>
</tr>
</tbody>
</table>

Table 7: approximate timescales for encounters of charged particles with grains computed using $\tau = 0.2$ (see text) in Equation 10. $T_e = T_i = 10$ K, grain radius = 0.1 $\mu$m.

4.2.3 An assessment of the effects of spontelectric grains

We consider here only one set of conditions, relevant to B68, namely $n_{\text{H}_2} = 10^3$ cm$^{-3}$, degree of ionization = $5 \times 10^{-4}$, $T = T_e = T_i = 10$ K, to investigate the outcome of the presence of spontelectric grains. We note that a variety of physical conditions may however be found in the literature for pre-stellar cores. For example the $n_{\text{H}_2}$ in pre-stellar cores vary between a few $10^4$ cm$^{-3}$ to $10^6$ cm$^{-3}$. The abundance of CO lies between $2.4 \times 10^{-5}$ in the core edge of L183 to the value of $8.5 \times 10^{-7}$ suggested for L1498 and L1517 B13. The degree of ionization may be as low as $2 \times 10^{-7}$ in L1544 but may be more than an order of magnitude higher in other regions.

We first show that the proportion of electrons removed directly from the gas phase to the surface of grains, due to their spontelectric nature, is small, for the conditions of B68. We use as a basis for our estimate the result gleaned from section 4.2.2 that the problem may be treated as an essentially static effect in which the accumulation of CO is offset instantaneously by the arrival of electrons, as shown in section 4.2.2. The charge, $q$, on a grain of radius $a$ with $n_{\text{ML}}$ monolayers of CO is given by $4\pi\alpha a^2 n_{\text{ML}} \phi$. Given that $n_{\text{ML}} = 12$ (section 4.2.1), the number of electrons attracted to each grain would be ~$5.75$. The number of grains, $n_G$ per m$^3$, is given by mass of the grains, equal to density of the grain material, $\delta$, times a grain volume, $4/3\pi a^3$, divided by the mass of gas, taking into account He, using a mass ratio of $\xi = 0.013$. Thus $n_G$ is given by $2.1 n_{\text{H}_2} \mu_0 \xi (\tau_{\text{rad}}/\delta)$ per m$^3$ = 0.73 m$^{-3}$. Therefore $0.73 \times 5.75 = 4.2$ electrons are removed per m$^3$, about 1% of the total given a value of $5 \times 10^9$ $n_{\text{H}_2}$ for the total ionization of the medium. Note that here we ignore the variation with the grain radius as CO accumulates, since only rough estimates are made. The assumption is implicit that each polarization charge on the grain has unit efficiency in removing an electron from the gas phase. We conclude that the ~12 ML layer of spontelectric CO (see Figure 5) has a resulting polarization sufficient to remove only ~1% of the electrons directly.

We consider a simple scenario which may govern the interaction of electrons with spontelectric grains. Initially, before any net adsorption of CO values in Table 7, lines 1 and 4, show that an electron or ion will encounter the grain on the timescale of between 1 and $2 \times 10^7$ seconds. The spontelectric effect, being a macroscopic non-local phenomenon, requires a certain film thickness to develop. We know from [9], that the effect is already active at 5 ML. Let us assume therefore that the spontelectric effect switches on at 5 ML, noting that the forthcoming argument does not turn upon this value. At this layer thickness, achieved after $1.18 \times 10^{12}$ seconds (see Figure 5), the CO-grain surface will then abruptly tend to a state with a surface voltage of ~$33$ mV. This is equivalent to $\sim 2.3$ charges on average. Note that here and subsequently we assume that the value of $\phi = 6.695 \times 10^{-3}$ V ML$^{-1}$ is roughly independent of temperature, see Table 5, and use the same value at 10 K as measured at 21 K. Thus the grain surface, initially 0.91 negative, will become abruptly 1.4 positive, that is, some grains will possess one positive charge and some two. The latter figure of two positive charges would decrease the characteristic time for electron-grain encounters to ~$2 \times 10^5$ seconds from the value of ~$3 \times 10^5$ seconds for a single positive charge (see Table 7). The grain surface then proceeds via electron collisions through a neutral state, requiring a further $10^9$ seconds (Table 7), and subsequently both ions and electrons will again encounter the grain on the 1 to $2 \times 10^7$ seconds timescale.

Now, however, a new mechanism intervenes in which ions and mobile electrons recombine on the grain surface. This has long since been proposed as an important catalytic mechanism for the removal of charge from the gas phase. If electrons are mobile on the grains, as we describe below, they will encounter and react with ions, creating neutrals. The electrons will initially be attracted, as the spontelectric effect becomes active, on the timescale of $3 \times 10^7$ seconds to the now positively polarization-charged grain. Ions will follow on the 1 to $2 \times 10^7$ second timescale and the cycle will be continuously repeated as the CO layer builds up. As these processes proceed, the grains will little by little accumulate an average positive polarization charge of 5.75, at 12 ML, which will be offset by electrons from the gas phase and accompanied by the same number of positive ions. Thus after ~$8 \times 10^{12}$ seconds have elapsed, the time required to give effectively complete CO adsorption (Figure 4), a state will be achieved with some well-defined average conditions, namely that in this state, each grain carries 5.75 electrons and an equal number of positive ions.

We now suggest that electrons and ions on the surface of the grain are continuously removed by recombination and continuously replenished from the gas phase, over a period of a further $6 \times 10^{12}$ seconds, where this time is taken from Figure 5. Surface recombination was discussed in detail in [57] and again in [39], in which major corrections to the
earlier publication were introduced. First however we discuss a phenomenological model and compare our results with those of [39] below. Surface recombination requires mobile electrons on the grain surface, a topic discussed in detail in [62]. It was shown there that an electron has a residence time at any absorption site of ~10^5 seconds, for a grain temperature of 10 K, whereupon it may tunnel typically ~ 20 nm to a new site. If we regard the tunnelling length as defining the diameter of an area swept out by an electron in any one tunnelling event, then an electron will effectively cover the entire grain surface in ~100 residence times, that is, ~ 10^3 seconds and recombine with a static ion in ~10^7 seconds. Thus in the absence of the spontelectric effect, with only 0.91 ion and 0.91 electron together on any one grain on average, recombination may therefore take place on a timescale of ~10^7 seconds. The rate of recombination of ions, i, and electrons, e, on the grain surface, per grain, will be proportional to [e] [i], where these represent numbers per grain. The increase in efficiency of recombination due to the spontelectric effect will therefore be (5.75/0.91)^2 ~ 40, relative to the recombination efficiency associated with non-spontelectric grains, reducing the time for recombination to ~2.5 × 10^5 seconds. A factor of 40^{1/2}, that is, 6.3 increase in efficiency, compared with non-spontelectric grains, will be passed on directly to reduce the degree of ionization of the medium. This may be seen as follows.

The degree of ionization in the gas phase is determined through a steady state balance between the rate of cosmic ray ionization per volume per second, ζ Howe, where ζ is typically ~3 × 10^{-17} s^{-1} (see for example [44]), and all loss processes through ion-electron recombination, both in the gas phase and at the grain surface. In the gas phase, recombination processes are very largely determined by e⁺ + H₂. Here H₂⁺ makes up ~0.2 of the total ionization⁴⁴, and the rate coefficient for recombination⁴⁴ is ~2 × 10^{-7} cm³ s⁻¹ giving an effective coefficient, k_{2nd}, of ~4 × 10^{-9} cm³ s⁻¹. If we balance this figure with ζ Howe, we obtain [e] = [ions] = ζ Howe/κ_{2nd}^{1/2} ~8.7 × 10^3 cm⁻³, yielding an ion fraction of ~8.7 × 10^{-8}, whereas our standard observed value in B68 is 5 × 10^{-9}. Thus gas phase removal rate, k_{2nd} [e] [ions], is too small to account for the low ionization in the medium.

We now compare this scenario with recombination on the grain surface. If the rate of loss of ionization on the surface of a single grain is given by κ s⁻¹, then the rate of loss = κ n_e cm⁻³ s⁻¹ = 7.26 × 10^{-12} n_{H2}κ, given the relationship between the number of grains per unit volume and the hydrogen number density (see above), where n_{H2} is here expressed per cm³. If we balance this with ζ Howe, ignoring gas phase recombination, then we require κ = 4.17 × 10^6 s⁻¹ or 2.4 × 10^5 seconds between recombinations. This is essentially the time that was estimated above as the interval between electron-ion encounters on a grain surface (~2.5 × 10^5 seconds), given on average 5.75 electrons and ions present.

Thus a model based on the presence of spontelectric grains in the medium gives essentially the same result as that which satisfies ζ n_{H2} = rate of destruction of charge, where the latter gives the observed degree of ionization. This demonstrates that the presence of spontelectric grains can indeed reproduce the unexpectedly low degrees of ionization in B68 and by implication in other prestellar cores.

If only 0.91 ions and electrons are present on average, that is, in the non-spontelectric case, we have seen above that κ is ~40 times smaller. Therefore in this case, the grain mechanism correspondingly fails by a factor of 6.3 to account for the degree of ionization observed. Thus we would suggest that the rate of removal of ions and electrons from the medium would, even under the circumstance of non-spontelectric grains, be governed by a dominant grain surface mechanism and a less effective gas phase mechanism. Taken together with the effect of the gas phase mechanism, which is ~7.5 less effective than the non-spontelectric grain surface mechanism, this yields a degree of ionization of ~3 × 10^{-8}, a figure not atypical for the degree of ionization in regions obscured from UV light.⁴⁴,⁶⁴

We now consider values of surface recombination rate coefficients based upon the theoretical models in [39], for comparison with the above estimates. We choose the model presented in [39] rather than that in [57], since, as noted above, [39] includes the very significant contribution of the polarization interaction between the grain and ions or electrons. The relevant equation is 5.15 of [39], which we note is sensitive to the choice of minimum grain size, to the power of -1.5, and also incorporates a significant contribution from very small grains, which may not be appropriate here⁶⁵.

At all events, in the present case we use the minimum radius of a grain as 10^8 m, the value quoted in [39] as appropriate to the standard ‘MRN’ power law size distribution for grains.⁶⁶. Introducing the relevant values of kinetic temperature (10K) and ion mass (H⁺) into equation 5.15 of [39] and equating the loss rate at the surface of a (non-spontelectric) grain with the cosmic ray production rate of ions as above, we find that the degree of ionization becomes ~2.8 × 10^{-8}, including the gas phase contribution. This figure is essentially the same as that of 3 × 10^{-8} deduced from the phenomenological model set out above for the non-spontelectric grain surface recombination case plus gas phase recombination. This agreement gives weight to our simple model.

We conclude that the effect of spontelectric grains is to enhance the removal of gas phase electrons and ions and thereby to reduce considerably the degree of ionization under the physical conditions associated with the pre-stellar core B68, in this case by a factor of ~6. There are some significant uncertainties in this estimate, perhaps principally in the assumption that the grain population can be adequately represented by a_{gr} = 0.1 μm. There is in fact growing observational evidence that the grain size distribution needs
to be modified in prestellar cores to include a greater population of larger grains.\textsuperscript{67,68} Thus in order to give more credence to the order of magnitude analysis presented above, the effects described should be incorporated into sophisticated time-dependent chemical models of pre-stellar cores, incorporating the latest data on grain size distribution. This is a problem well worth addressing since, in connection with the low ionization fraction found in pre-stellar cores, many such regions support a considerably weaker magnetic field than would be predicted by the standard empirical relationship $B = b n_0^{3/2}$ $\mu$G, where $b = 1$ to 5 and $n_0 = 2 n_{12} + n_{10}$. For example, in the prestellar cores L1498 and L1517B, fields are $10 \pm 5$ and $30 \pm 10$ $\mu$G, respectively, whereas the derived densities are $10^{3}$ cm$^{-3}$ and $6 \times 10^{5}$ cm$^{-3}$, suggesting fields of $>300$ or $>800$ $\mu$G. Since magnetic fields in the medium are set up through moving charges, a reduction in ion and electron density through a sizeable factor, through the action of spontelectric grains, may contribute to the weakness of the magnetic field. This will be accompanied by a loss of magnetic pressure to withstand gravitational collapse. There are a number of other areas in which the reduction of the degree of ionization will affect star formation, for example the loss of angular momentum from the gas to the grains, and the release of CO from the grain on warming, as a protostar forms, and the accompanying re-establishment of a larger magnetic field.

5. Summary and concluding comments

The main thrust of this paper is the experimental work which verifies that solid CO on water ice is spontelectric and shows that the magnitude of the spontelectric field depends on the nature of the ice on which the material is laid down. We find that relative to CO on a SiO$_2$ substrate\textsuperscript{6}, the strength of the spontelectric field is in the ratio $1 : 0.76 : 0.52$ for CO-p$_{ASW}$, CO-CSW and CO-$c_{ASW}$ respectively, for a deposition temperature of 20K for CO-p$_{ASW}$ and CO-CSW and 21K for CO-$c_{ASW}$.

The choice of substrates was made with a view to astrophysical applications. The normal circumstance in molecular clouds is that grains possess on average a single negative charge, given that they are shielded from an ultraviolet field. If the temperature is $\leq$100K, then observations show that grains tend to be coated with $c_{ASW}$\textsuperscript{67}. As the temperature falls below $\sim$26K, we have shown that a total of 12 ML of spontelectric CO ice can form on this substrate on a time scale about half of that of the expected lifetime of the prestellar phase of star formation, under the conditions of $10^7$ H$_2$ cm$^{-3}$ and $T = 10$K, representative of the pre-stellar core B68. The net result of the CO ice is that grains become spontelectric, attracting electrons and positive ions to their surface, where these species undergo recombination. This reveals a spontelectric grain as essentially a catalyst for the removal of ionization from the gas phase. The spontelectric grain surface recombination mechanism takes over from the gas phase recombination of $e^-$ + H$_2$, plus the non-spontelectric grain surface mechanism, as the dominant means of removing ions and electrons from the medium. Put succinctly, cosmic rays are the source for ionization and spontelectric grains now provide the major sink. This results in values of fractional ionization relative to H$_2$ of $5 \times 10^{-6}$ in B68, compared with the more familiar value of $3 \times 10^{-9}$ in molecular cloud cores.\textsuperscript{69,70,71} In general the degree of ionization is reduced by a factor equal to the number of electrons (or ions) trapped in the steady state on the spontelectric grain surface, given some grain radius. Here we have used the standard value for the bare grain of $a_0 = 0.1$ $\mu$m, giving in B68 the number of trapped electrons or ions equals $\sim$6, where such a steady state value is established after $\sim$2.5 $\times$ 10$^5$ years. The presence of spontelectric grains may indeed be the root of the low ionization fraction observed in prestellar cores in general, where these show strong CO depletion. This should however most properly be seen as a postulate rather than a proof, since it is possible that other general explanations for a contribution to low fractional ionizations may be forthcoming. A contributory factor may for example be a reduction of the cosmic ray ionization rates in dense regions, which according to [72] fall by between 25% and 40% in the prestellar cores L1498 and L1517B.

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